



PQC 부채널 분석

2019년 07월 17일 (금)

국민대학교

발표자 : 심보연

PKC (Public Key Cryptosystem)

RSA, ECC

Factoring and Discrete Logarithms



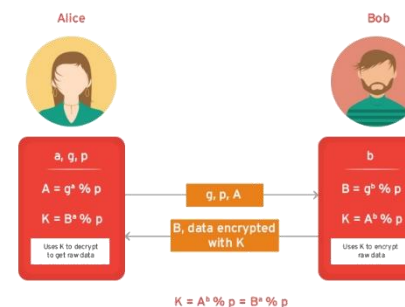
Certificate



Smart Car



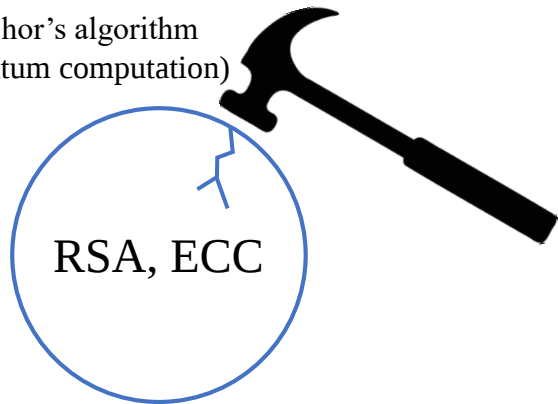
e-Passport



Key Exchange

■ PKC (Public Key Cryptosystem)

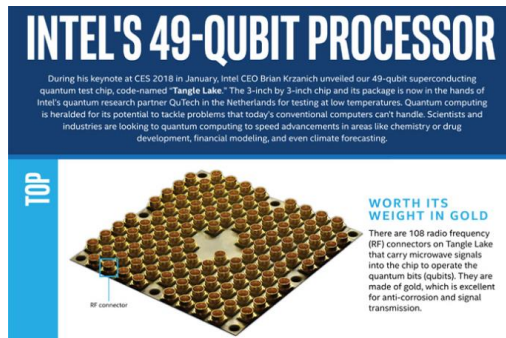
1994 Shor's algorithm
(for quantum computation)



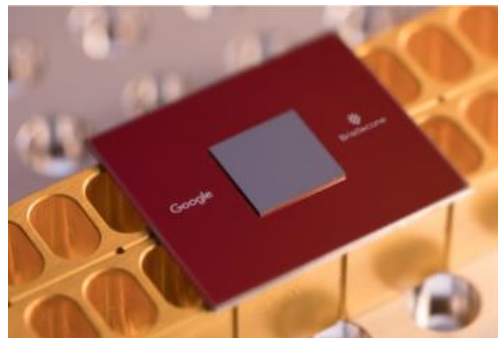
Quantum
Computer

estimated to arrive in the next 10 to 15 years

Factoring and Discrete Logarithms



49-qubit chip
"Tangle-Lake"
January 2018



72-qubit chip
"Bristlecone"
March 2018

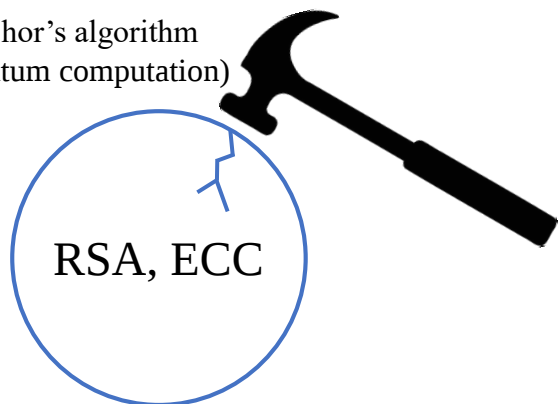


53-qubit quantum computer
"Q System One"
January 2019

[1] Peter Williston Shor, "Algorithms for Quantum Computation: Discrete Logarithms and Factoring", SFCS 1994, pp. 124-134, 1994.

■ PKC (Public Key Cryptosystem)

1994 Shor's algorithm
(for quantum computation)

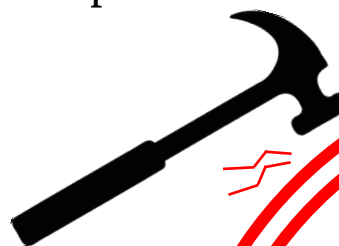


Factoring and Discrete Logarithms

KEM/Encryption

Signature

Quantum
Computer



Lattice-based

Code-based

Post-Quantum
Cryptography

Multivariate

Hash-based

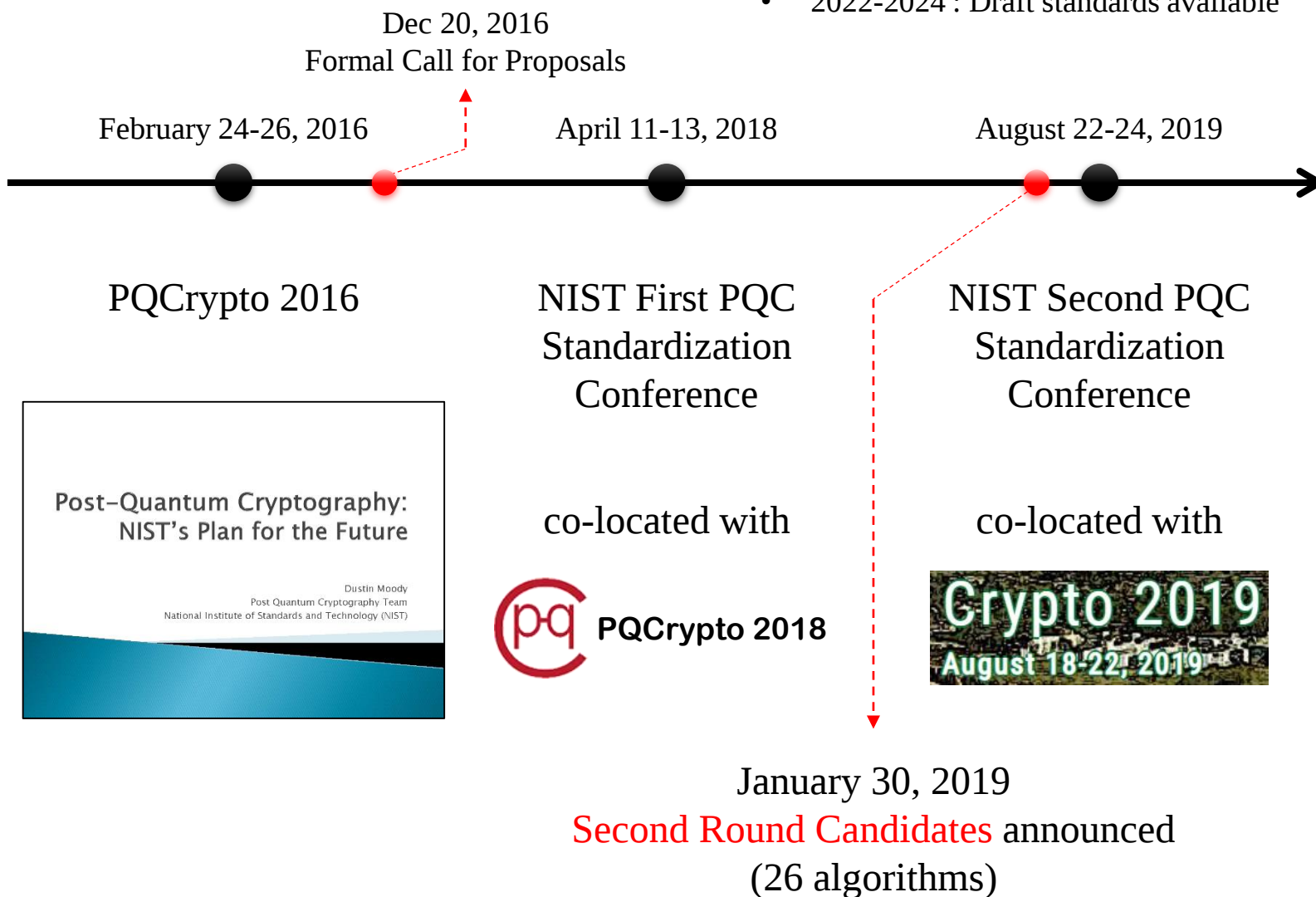
Isogeny

etc.

[1] Peter Williston Shor, "Algorithms for Quantum Computation: Discrete Logarithms and Factoring", SFCS 1994, pp. 124-134, 1994.

PKC (Public Key Cryptosystem)

- 2020/2021 : Select algorithms or start a 3rd Round
- 2022-2024 : Draft standards available



■ NIST Round 2 Candidates

KEM/Encryption

(9) Lattice-based		(7) Code-based	
FrodoKEM	LWE	Classic McEliece	Goppa
LAC	RLWE	NTS-KEM	Goppa
NewHope	RLWE	BIKE	Short Hamming
Round5	LWR/RLWR	HQC	Short Hamming
Crystals-Kyber	MLWE	LEDACrypt	Short Hamming
Saber	MLWR	RQC	Low rank
Three Bears	IMLWE	ROLLO	Low rank
NTRU	NTRU	(1) Isogeny	
NTRU Prime	NTRU	SIKE	Isogeny

Signature

(3) Lattice-based	
qTESLA	Fiat-Shamir
Crystals-Dilithium	Fiat-Shamir
FALCON	Hash then sign
(4) Multivariate	
GeMMS	HFE
LUOV	UOV
Rainbow	UOV
MQDSS	Fiat-Shamir
(2) Symmetric-based	
SPHINCS+	Hash
Picnic	ZKP

■ NIST PQC Standardization

❖ The selection criteria

➤ Security

- ✓ against both classical and quantum attacks

➤ Performance

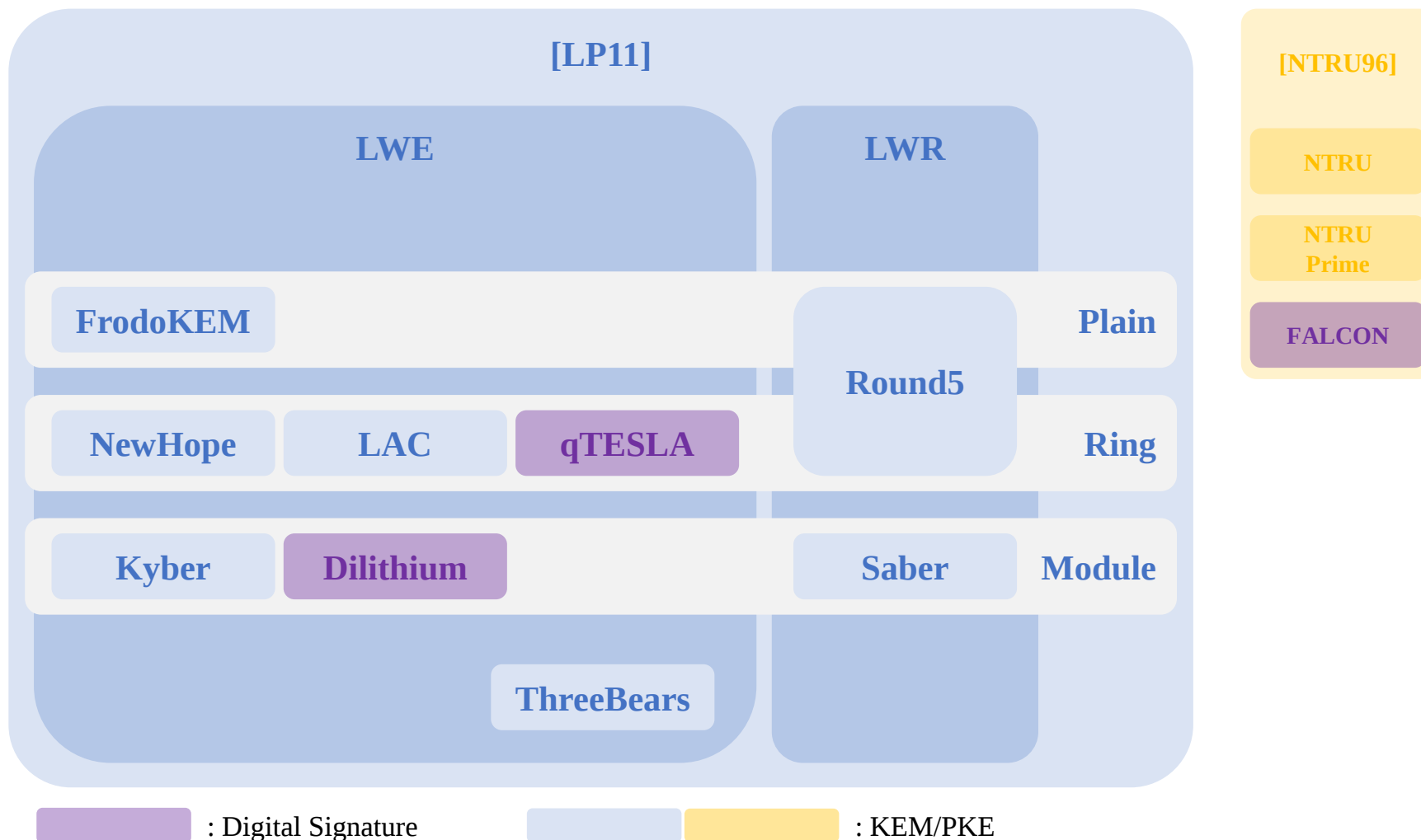
- ✓ measured on various “classical” platforms

➤ Other properties

- ✓ Drop-in replacements – Compatibility with existing protocols and networks
- ✓ Perfect forward secrecy
- ✓ Resistance to side-channel attacks
- ✓ Simplicity and flexibility
- ✓ Misuse resistance



■ NIST Round 2 Candidates : Lattice-based



[LP11] Richard Lindner and Chris Peikert, “Better Key Sizes (and Attacks) for LWE-Based Encryption”, CT-RSA 2011, pp. 319-339.

[NTRU96] Jeffrey Hoffstein, Jill Pipher, and Joseph H. Silverman, “NTRU: A Ring-Based Public Key Cryptosystem”, ANTS 1998, pp.267-288.

SCA on KEM/PKE

※ Convolution product = Polynomial multiplication

공격 대상	공격 연산	공격 유형	대응 기법
NTRU	Decryption (Difference in #hash calls)	TA	Fixed hash calls
NTRU	Decryption (Polynomial multiplication)	DPA	
NTRU	Decryption (Polynomial multiplication)	SPA, CPA, SOCPA	Masking, Blinding
NTRU	Protected Decryption [IEICE 2011] (Polynomial multiplication)	CA	
NTRU	Protected Decryption [IEICE 2011] (Polynomial multiplication)	Chosen Ciphertext DPA	Chosen dummy, Masking, Blinding
Knuth-Yao Sampler	Bit scanning		Shuffling
Ring-LWE scheme			Masking
Ring-LWE scheme	Decryption (Addition)	Chosen Ciphertext SPA	
Ring-LWE scheme	Decryption (Multiplication, addition)	CPA	Masking
Ring-LWE scheme	Decryption (Multiplication, addition)	CPA	Additively Homomorphic Masking
Ring-LWE scheme	Protected Decryption (masking) (NTT)	TA ^p	Shuffling
NTRU	Decryption (Polynomial multiplication)	SPA, CPA, SOCPA, CA	Random Key Rotation
FrodoKEM, Lizard	Constant-time CDT sampler	SPA	Look-up table based
NTRU (NIST Round 1)	Decryption (Polynomial multiplication)	CA	Constant-time, Initialization with a random

Polynomial multiplication & Sampler

[CT-RSA 2007]

[RFID Security 2008]

[IEICE 2010]

FA [IEICE 2011]

FA [Cryptography and Communications 2012]

[Microprocessors and Microsystems 2013]

[TIIS 2013]

[ePrint 2014]

[CHES 2015]

[AsianHOST 2016]

[J. Cryptographic Engineering 2016]

[PQCrypto 2016]

[CHES 2017]

[Computers and Electrical Engineering 2017]

[Applied Science 2018]

[Applied Science 2018]

※ Convolution product = Polynomial multiplication

SCA on KEM/PKE

공격 대상	공격 연산	공격 유형	대응 기법
Binary Ring-LWE scheme	Decryption (Polynomial multiplication)	SPA, DPA	Dummy and memory update, Masking
FrodoKEM, NewHope	Encryption (Multiplication)	Horizontal CPA	Shuffling, Insert dummy
FrodoKEM	Encryption (Multiplication)	TA ^p	Shuffling, reduce algorithmic variance
NewHope	Decryption (Key mismatch oracle)	Key reuse based SPA, FA	
Ring-LWE scheme	Protected Decryption (masking) (NTT)	TA ^p	Masking
LAC, Ramstake	Decryption (Decoding of error correcting code)	Chosen Ciphertext TA	
Frodo, LAC, Round5, NTRU-HPS		TA ^p (SAC 2018) + Algebraic	
NewHope	Encryption (Message Encoding)	SPA, TA ^p	Masking + Shuffling
NTRU Prime	Decryption (Polynomial Multiplication)	SPA, Chosen-input SPA, Online TA ^p , Vertical CPA, Horizontal In-Depth CPA	(Masking, Blinding) + Shuffling
Round5, LAC, Kyber, NewHope, Saber, FrodoKEM	Decryption (FO transform, decoding ECC)	Chosen Ciphertext SPA	



[DATE 2018]

[GLSVLS 2018]

[IEEE Trans. on Computer 2018]

[HOST 2018]

[SAC 2018]

[TCHES 2018]

[TCHES 2018]

[CT-RSA 2019]

[Latincrypt 2019]

[TIS 2019]

[ePrint 2020]

[PQCrypto 2020]

[TCHES 2020]

[TCHES 2020]

■ [HOST 2018], [SAC 2018]

❖ Attack Scenario

Generate *seed*

$a \leftarrow \text{GenA}(\text{seed})$

$s, e \leftarrow \text{sample}()$

$b = as + e$

Single-Trace Attack

Public (b, seed) , private (s)

$v' = b's$

$V = \text{Rec}(v', r)$

Alice

Bob

(b, seed)

(b', r)

$s', e', e'' \leftarrow \text{sample}()$

$a \leftarrow \text{GenA}(\text{seed})$

$b' = as' + e'$

$v = bs' + e''$

$r = \text{sample}'(v)$

$V = \text{Rec}(v, r)$

$ss_{key} = \text{SHA256}(V)$

ss_{key} : shared secret key

$ss_{key} = \text{SHA256}(V)$



[1] Aydin Aysu, Youssef Tobah, Mohit Tiwari, Andreas Gerstlauer, and Michael Orshansky, "Horizontal Side-Channel Vulnerabilities of Post-Quantum Key Exchange Protocols", HOST 2018, pp. 81-88, April, 2018.

[2] Joppe W. Bos, Simon Friedberger, Marco Martinoli, Elisabeth Oswald, and Martijn Stam, "Assessing the Feasibility of Single Trace Power Analysis of Frodo", SAC 2018, pp. 261-234, August, 2018.

■ [HOST 2018], [SAC 2018]

[HOST 2018] Horizontal Side-Channel Vulnerabilities of Post-Quantum Key Exchange Protocols

[SAC 2018] Assessing the feasibility of single trace power analysis of Frodo

	[HOST 2018]	[SAC 2018]
Target Scheme	FrodoKEM, NewHope	FrodoKEM
Target Operation	Matrix Multiplication (<i>AS</i>)	Matrix-vector Multiplication (<i>As</i>)
	Schoolbook Multiplication with Barret reduction (<i>as</i>)	
Implementation	Hardware (SAKURA-G)	Software (ELMO simulation – ARM Cortex M0)
Power Model	Hamming Distance	Hamming Weight
Attack Type	Horizontal Correlation Power Analysis	Divide-and-Conquer Template Attack
		Extend-and-Prune Template Attack
# Traces	Single-Trace	Single-Trace
Countermeasure	Shuffling, Insert dummy	Shuffling / reduce algorithmic variance

[ePrint 2020] LWE with Side Information; Attacks and Concrete Security Estimation

※ Convolution product = Polynomial multiplication

SCA on KEM/PKE

공격 대상	공격 연산	공격 유형	대응 기법
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Round5, LAC, Kyber, NewHope, Saber, FrodoKEM	Decryption (FO transform, decoding ECC)	Chosen Ciphertext SPA	



[DATE 2018]

[GLSVLS 2018]

[IEEE Trans. on Computer 2018]

[HOST 2018]

[SAC 2018]

[TCHES 2018]

[TCHES 2018]

[CT-RSA 2019]

[Latincrypt 2019]

[TIS 2019]

[ePrint 2020]

[PQCrypto 2020]

[TCHES 2020]

[TCHES 2020]

■ [PQCrypto 2020] Defeating NewHope with a Single-Trace

❖ Attack Scenario

μ : secret message

$a \leftarrow \text{GenA}(\text{seed})$

$s', e', e'' \leftarrow \text{sample}()$

$u \leftarrow as' + e'$

$v \leftarrow bs' + e'' + \text{Encode}(\mu)$

$h \leftarrow \text{Compress}(v)$

Single-Trace Attack

Alice

Bob

(u, h)

NewHope : Key Generation

Input

Output

Public key (b, seed) , private key (s)

1. Generate seed

2. $a \leftarrow \text{GenA}(\text{seed})$

3. $s, e \leftarrow \text{sample}()$

4. $b = as + e$

5. Return $(b, \text{seed}), (s)$

$v \leftarrow \text{Decompress}(h)$

$\mu \leftarrow \text{Decode}(v - us)$

$ss_{key} = \text{SHAKE256}(\mu)$

ss_{key} : shared secret key

$ss_{key} = \text{SHAKE256}(\mu)$



■ [PQCrypto 2020] Defeating NewHope with a Single-Trace

펄스 없으면
공격 성공률 100%

Optimization Level 0

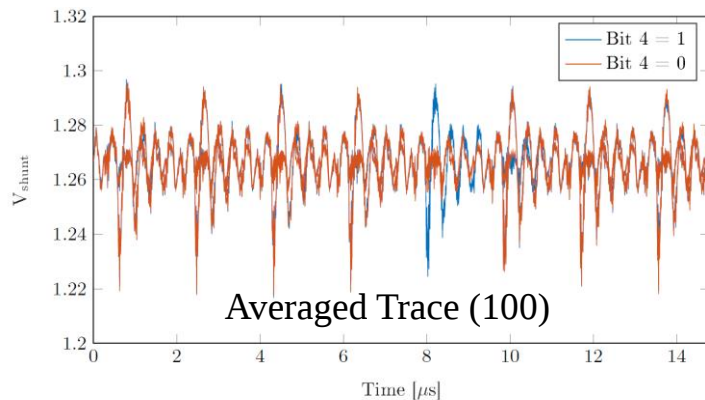
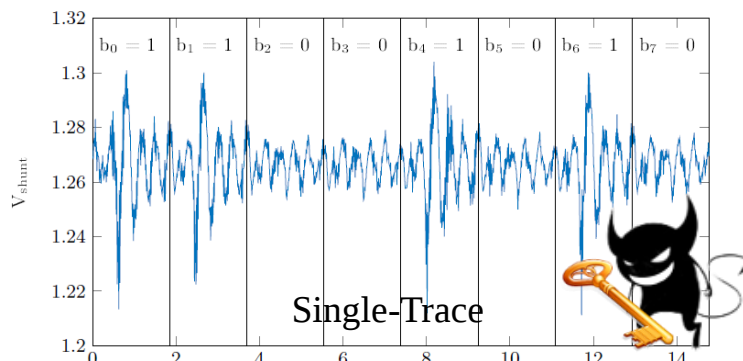


Fig. 2. Measurement traces on top of each other. Every trace is 100 times averaged. Code compiled with optimization disabled.



47% 펄스 → 후처리 없어도 99.5%

Fig. 3. A single trace measurement where message byte 1 is set to the value 83 (binary 01010011). Code compiled with optimization disabled.

Optimization Level 3

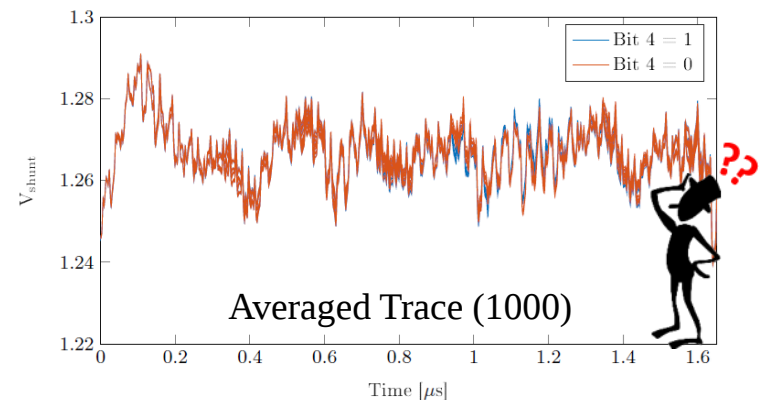
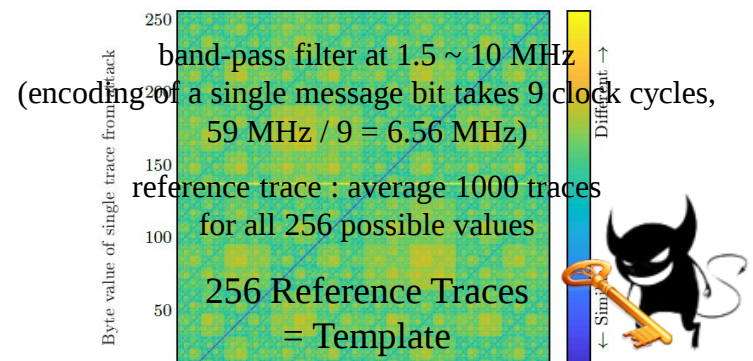


Fig. 4. All measurement traces on top of each other. Every trace is 1000 times averaged. Code compiled with optimization enabled (O3).



4% 펄스 → 2-byte 전수조사 → > 99%

Fig. 5. Similarity between a single power trace compared to the reference traces.

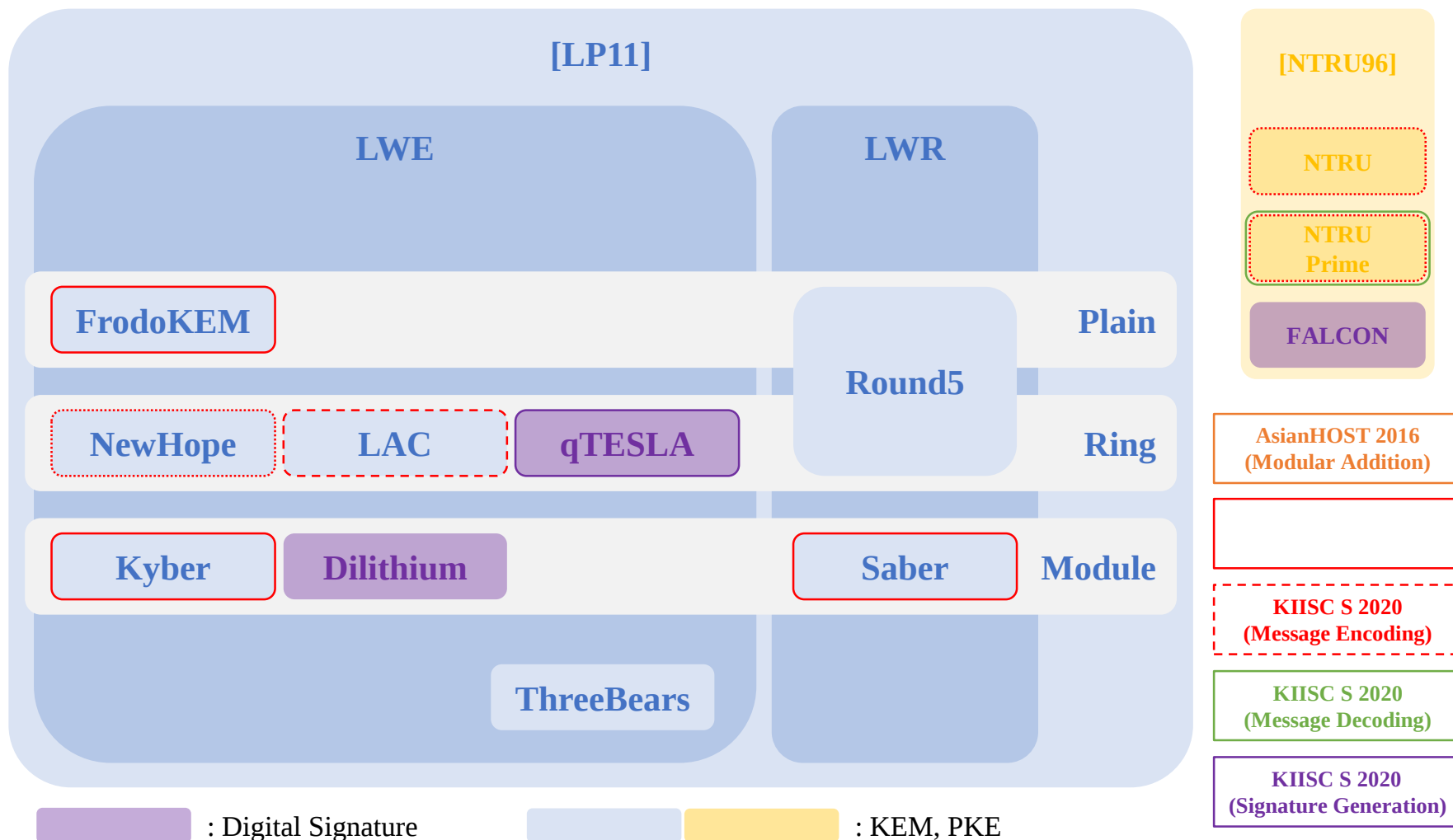
SCA on Signature

공격 대상	공격 연산	공격 유형	대응 기법
NTRUSign	Sign Generation	FA	
BLISS	Gaussian Sampling, Rejection Sampling	CA	
BLISS, ring-TESLA, GLP	Key Generation, Sign Generation, Verification	FA	
BLISS, TESLA, GLP, GPV	Gaussian Sampling	CA	
BLISS	Polynomial multiplication, Gaussian Sampling		
BLISS	Gaussian Sampling		
BLISS	Rejection Sampling, Gaussian Sampling, Polynomial multiplication	SPA, SEMA, BTA	
	Gaussian Sampling	CA	
Dilithium, qTESLA	Sign Generation	FA	
GLP			Masking
BLISS	Rejection Sampling	TA	
Dilithium			Masking
qTESLA			Masking

Polynomial multiplication & Sampler

- [Cryptography and Communications 2012]
- [CHES 2016]
- [FDTC 2016]
- [SAC 2016]
- [ICAR 2016]
- [ePrint 2017]
- [SAC 2017]
- [SAC 2017]
- [IACR 2018]
- [EUROCRYPT 2018]
- [ICAR 2019]
- [ePrint 2019]
- [CARDIS 2019]

■ NIST Round 2 Lattice



[LP11] Richard Lindner and Chris Peikert, "Better Key Sizes (and Attacks) for LWE-Based Encryption", CT-RSA 2011, pp. 319-339.

[NTRU96] Jeffrey Hoffstein, Jill Pipher, and Joseph H. Silverman, "NTRU: A Ring-Based Public Key Cryptosystem", ANTS 1998, pp.267-288.

Our results

Conference	Title / Description
AsianHOST 2016	Chosen ciphertext Simple Power Analysis on software 8-bit implementation of ring-LWE encryption
KIISC S2020	NIST Round 2 후보 LAC Key Encapsulation Mechanism에 대한 신규 단일 파형 공격
	LAC / Message Encoding
	NIST Round 2 후보 격자 기반 KEM NTRU LPRime에 대한 신규 단일 파형 공격
	NTRU LPRime / Message Decoding
	NIST Round 2 후보 마스킹된 qTESLA 전자서명 알고리즘에 대한 단일 파형 공격
	qTESLA / Signature Generation

Chosen ciphertext SPA attack on ring-LWE encryption scheme

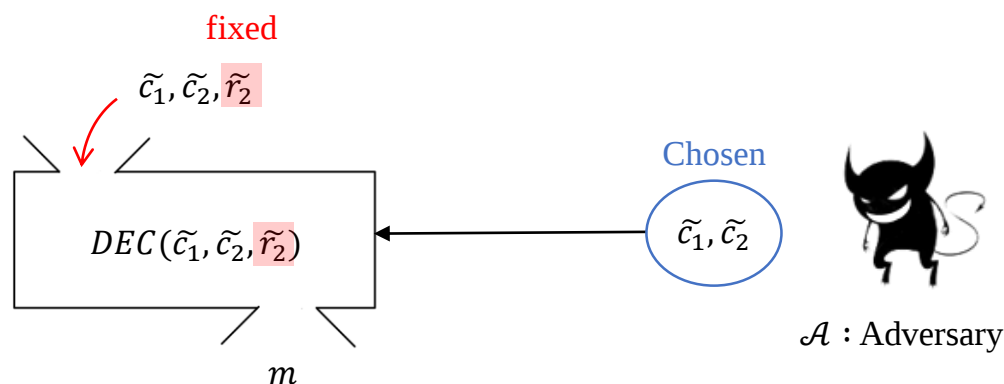
Attack Scenario

: Private key

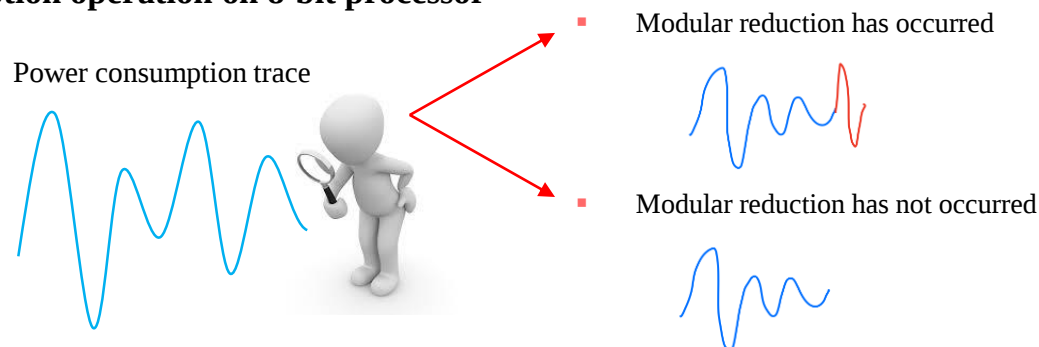
: Public key

Algorithm. Pseudo-code of Decryption	
Input	$(\tilde{c}_1, \tilde{c}_2), (\tilde{r}_2)$
Output	Message m
<pre> 1. for $i = 0$ to $n - 1$ do 2. $TC_1[i] \leftarrow \tilde{c}_1[i] \times \tilde{r}_2[i]$ 3. if $TC_1[i] \geq q$ then 4. $TC_1[i] \leftarrow TC_1[i] \bmod q$ 5. end if 6. $M'[i] \leftarrow TC_1[i] + \tilde{c}_2[i]$ 7. if $M'[i] \geq q$ then 8. $m'[i] \leftarrow M'[i] \bmod q$ 9. else 10. $m'[i] \leftarrow M'[i]$ 11. end if 12. $m' \leftarrow INTT(m')$ 13. $m \leftarrow \text{Decode}(m')$ 14. end for </pre>	

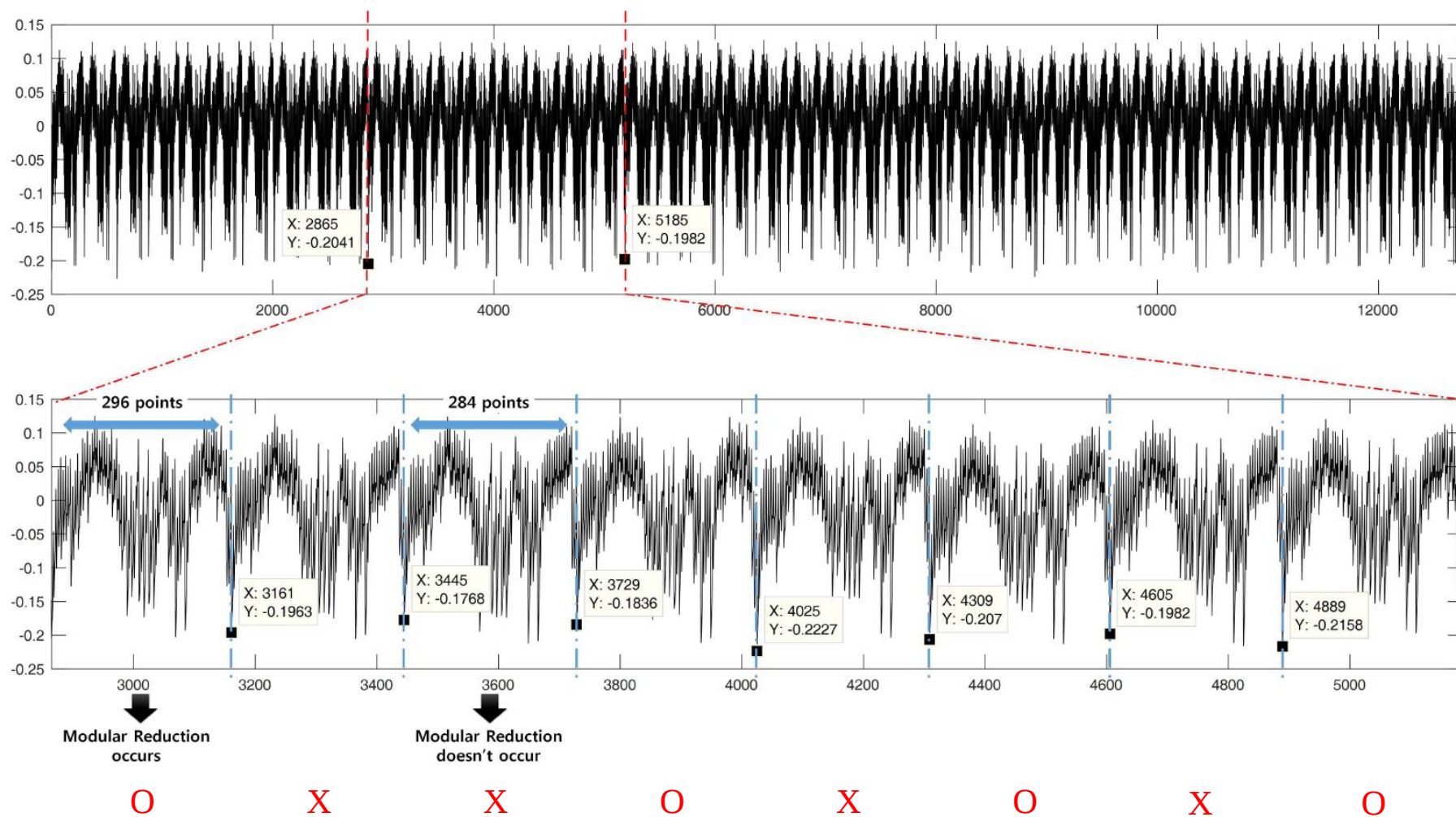
➤ The adversary can select different ciphertexts (= chosen ciphertexts)



➤ The adversary can measure their power consumption during decryption operation on 8-bit processor

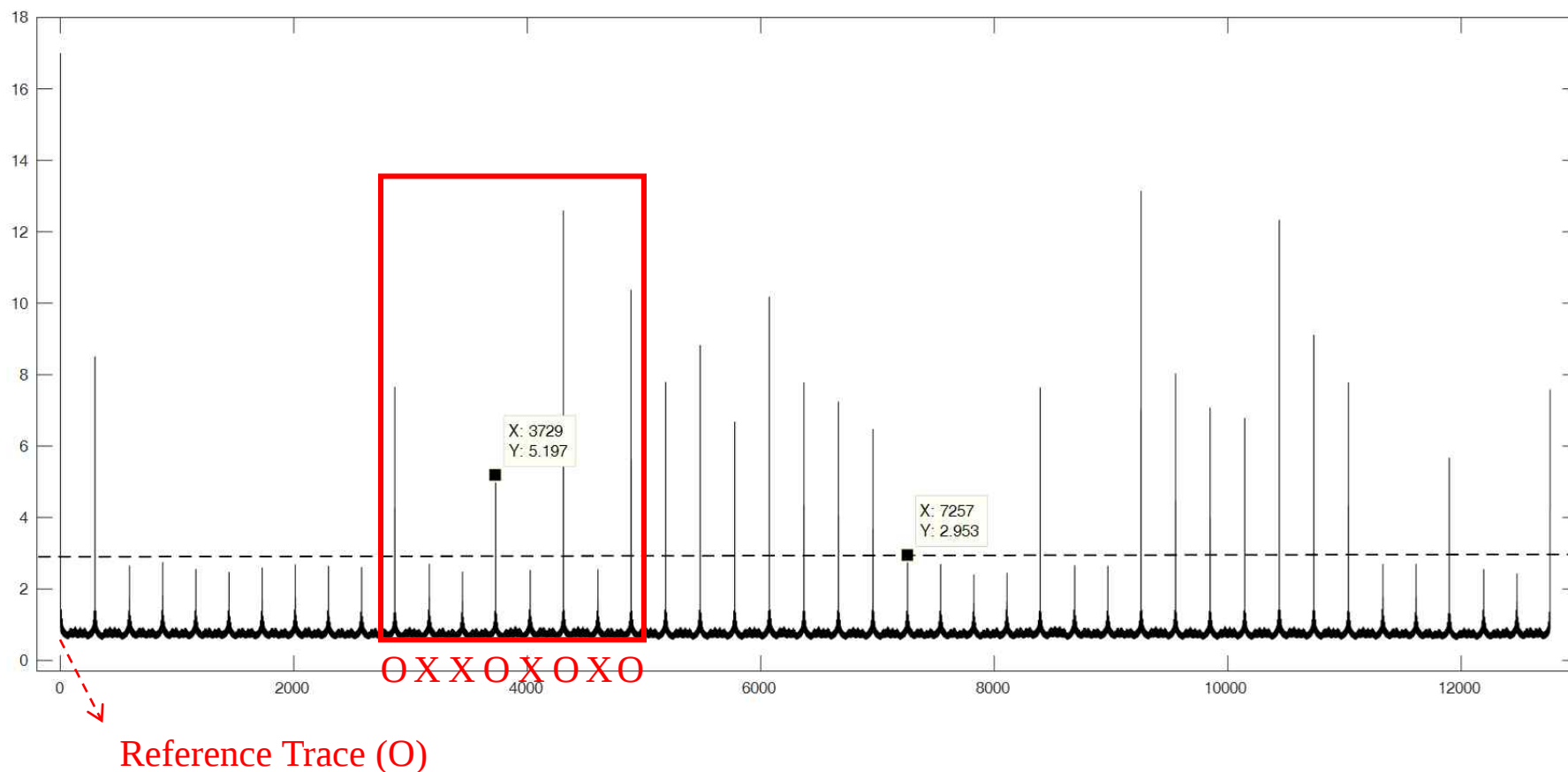


■ Is it possible to **distinguish** whether a modular operation occurs or not?



■ Is it possible to **distinguish** whether a modular operation occurs or not?

❖ $\text{PCDC}(X, Y) = \sigma(X) / \sigma(X - Y)$



- 박애선, 원유승, 한동국, “8 비트 구현 Ring-LWE 암호시스템의 SPA 취약점 연구”, 한국정보보호학회 논문지, 2017.
- Countermeasure : 박애선, 원유승, 한동국, “Ring-LWE 기반 공개키 암호시스템의 선택 암호문 단순전력분석 공격 대응법”, 한국정보보호학회 논문지, 2017.

■ LAC

❖ Attack Scenario

μ : secret message

$a \leftarrow \text{GenA}(\text{seed})$

$\mu' \leftarrow \text{ECC}_{\text{BCH}}(\mu)$

$s', e', e'' \leftarrow \text{sample}()$

$u \leftarrow as' + e'$

$v \leftarrow bs' + e'' + \text{Encode}(\mu')$

Single-Trace Attack

Alice

Bob

(u, v)

LAC : Key Generation

Input

Output

Public key (b, seed) , private key (s)

1. Generate seed

2. $a \leftarrow \text{GenA}(\text{seed})$

3. $s, e \leftarrow \text{sample}()$

4. $b = as + e$

5. Return $(b, \text{seed}), (s)$

$\mu' \leftarrow \text{Decode}(v - us)$

$\mu \leftarrow \text{ECC}_{\text{BCH}}^{-1}(\mu')$

$ss_{\text{key}} = \text{HASH}(\mu, u, v)$

ss_{key} : shared secret key

$ss_{\text{key}} = \text{HASH}(\mu, u, v)$



■ LAC : Message Encoding

```

#define RATIO 125

//D2 encoding
#ifdef LAC256

//compute the length of c2
c2_len=(mlen+ECC_LEN)*8*2;
//generate error vector e2
gen_psi_std(e2,c2_len,seeds+2*SEED_LEN);

int vec_bound=c2_len/2;
int8_t message;
//compute code*q/2+e2,
for(i=0;i<vec_bound;i++)
{
    //RATIO=q/2. add code*q/2 to e2
    message=RATIO*((p_code[i/8]>>(i*8))&1);
    e2[i]=e2[i]+message;
    //D2 encode, repeat at i+vec_bound
    e2[i+vec_bound]=e2[i+vec_bound]+message;
}

#else

//compute the length of c2
c2_len=(mlen+ECC_LEN)*8;
//generate error vector e2
gen_psi_std(e2,c2_len,seeds+2*SEED_LEN);
//compute code*q/2+e2,
for(i=0;i<c2_len;i++)
{
    //RATIO=q/2. add code*q/2 to e2
    e2[i]=e2[i]+RATIO*((p_code[i/8]>>(i*8))&1);
}
#endif

//c2=b*r+e2+m*[q/2]
poly_aff(pk+SEED_LEN,r,e2,c2,c2_len);
//compress c2
poly_compress(c2,c+DIM_N,c2_len);
*clen=DIM_N+c2_len/2;
  
```

Encapsulation

μ : secret message

$a \leftarrow \text{GenA}(\text{seed})$

$\mu' \leftarrow \text{ECC}_{\text{BCH}}(\mu)$

$s', e', e'' \leftarrow \text{sample}()$

$u \leftarrow as' + e'$

$v \leftarrow bs' + e'' + \text{Encode}(\mu')$

Single-Trace Attack

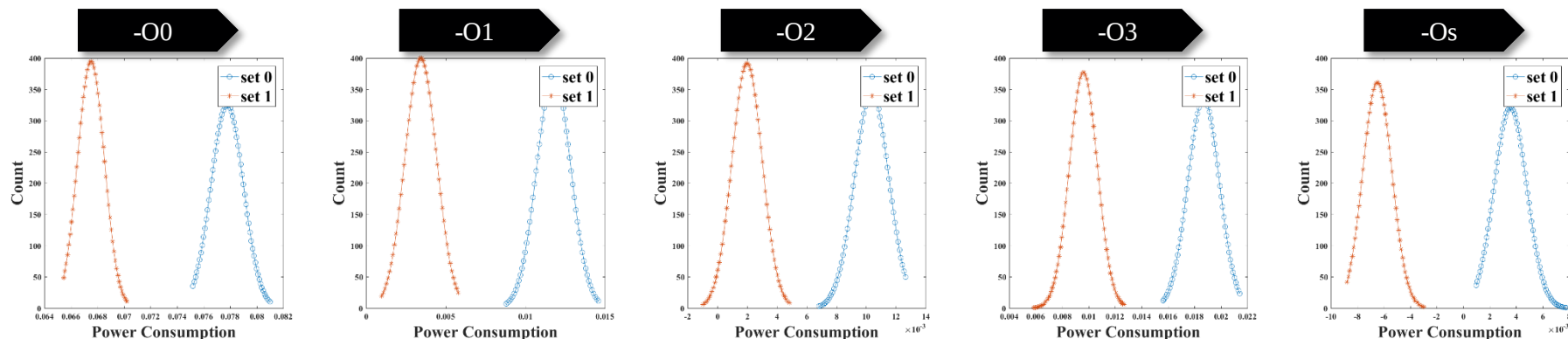
$p_code = \mu' = (\mu \parallel ecc)$

Secret Message $\mu \in \{0,1\}^I, I = 256$

Error Correcting Code $ecc \in \{0,1\}^l, l = 144$

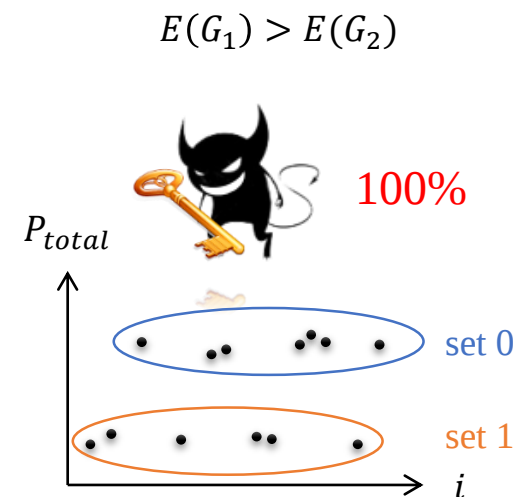
$message = \begin{cases} 0x00, & \text{if } (p_code[i] \gg j) \wedge 1 = 0 \\ 0x7d, & \text{if } (p_code[i] \gg j) \wedge 1 = 1 \end{cases}$

■ LAC : Distributions of the PoIs



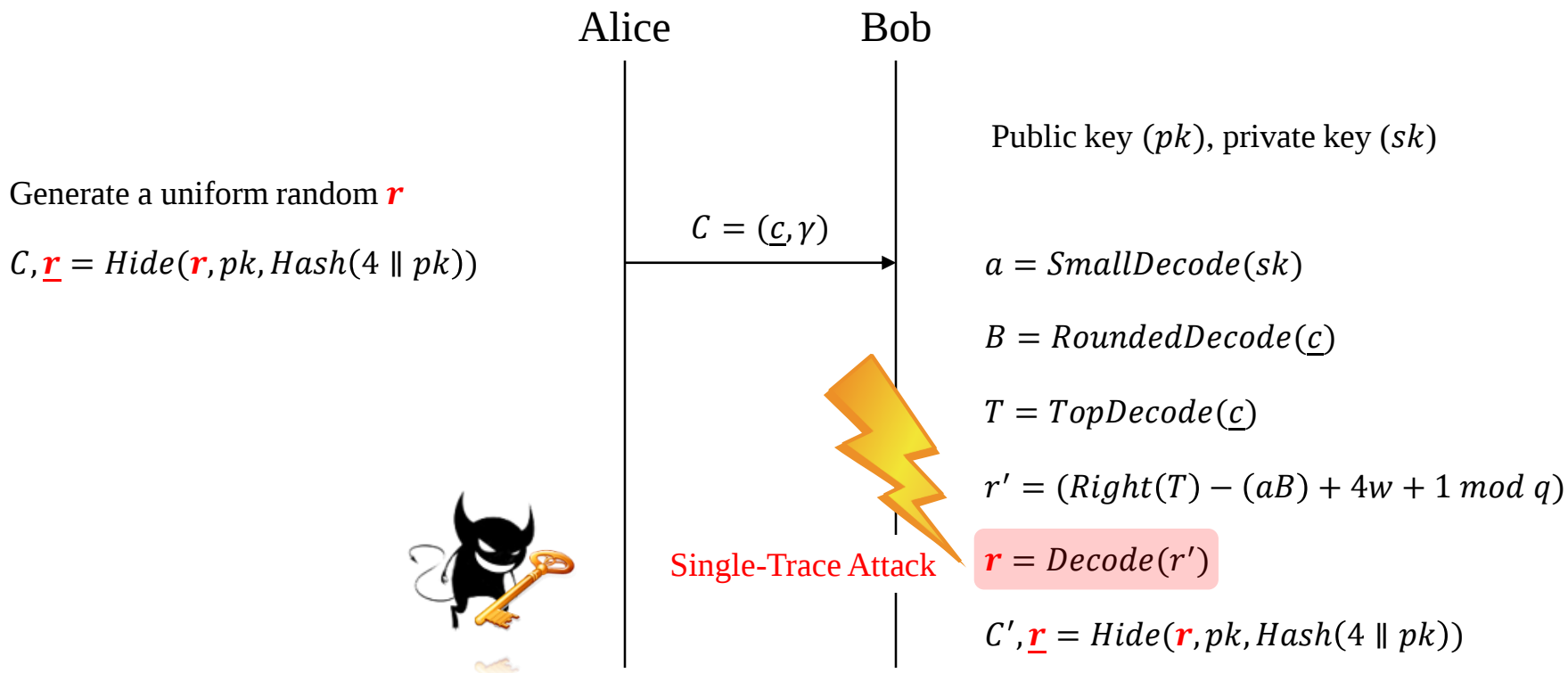
Optimization Level	$E(G_1)$	$E(G_2)$	$ E(G_1) - E(G_2) $
-O0	7.7773e-02	6.7497e-02	1.0276e-02
-O1	1.1788e-02	3.4290e-03	8.3590e-03
-O2	1.0367e-02	1.9882e-03	8.3788e-03
-O3	1.8690e-02	9.5977e-03	9.0923e-03
-Os	3.5680e-03	-6.4983e-03	1.0066e-04

k-means clustering algorithm



■ NTRU Prime / LPRime

❖ Attack Scenario



■ NTRU Prime / LPRime : Message Decoding

❖ Decrypt

```

/* return -1 if x<0; otherwise return 0 */
static int int16_negative_mask(int16 x)
{
    uint16 u = x;
    u >>= 15;
    return -(int) u;
    /* alternative with gcc -fwrapv: */
    /* x>>15 compiles to CPU's arithmetic right shift */
}

/* r = Decrypt((B,T),a) */
static void Decrypt(int8 *r,const Fq *B,const int8 *T,const small *a)
{
    Fq aB[p];
    int i;

    Rq_mult_small(aB,B,a);
    for (i = 0;i < I;++i)
        r[i] = -int16_negative_mask(Fq_freeze(Right(T[i])-aB[i]+4*w+1));
}

#define XDecrypt Decrypt

/* r = ZDecrypt(C,sk) */
static void ZDecrypt(Inputs r,const unsigned char *c,const unsigned char *sk)
{
    small a[p];
    Fq B[p];
    int8 T[I];

    Small_decode(a,sk);
    Rounded_decode(B,c);
    Top_decode(T,c+Rounded_bytes);
    XDecrypt(r,B,T,a);
}

```

Decapsulation

 $a = \text{SmallDecode}(sk)$
 $B = \text{RoundedDecode}(c)$
 $T = \text{TopDecode}(c)$
 $r' = (\text{Right}(T) - (aB) + 4w + 1 \bmod q)$
 $r = \text{Decode}(r')$
 $C', r = \text{Hide}(r, pk, \text{Hash}(4 \parallel pk))$

Single-Trace Attack

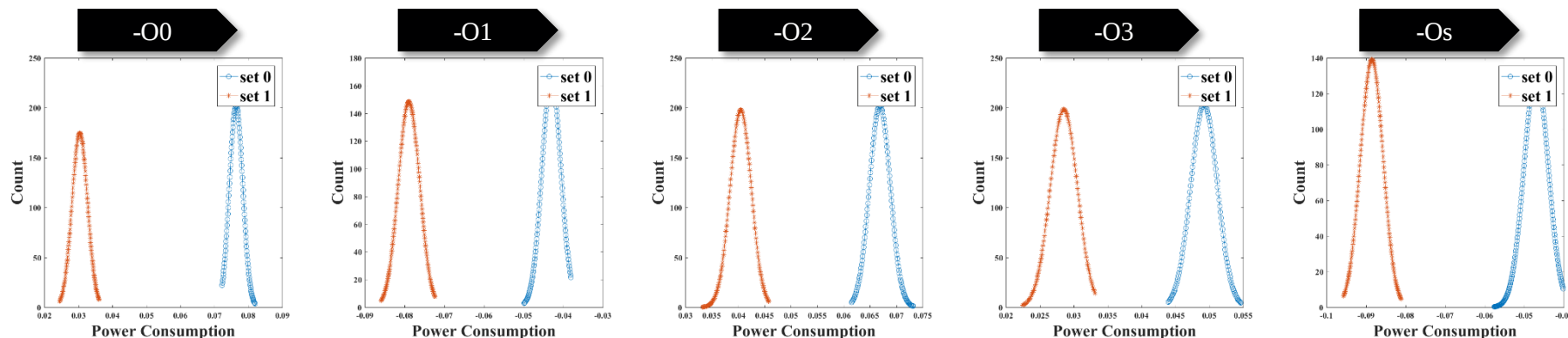
Secret Message $r \in \{0,1\}^I, I = 256$

 $r = (r_0, \dots, r_{I-1})_2, r_i = r[i]$

$$\text{int16_negative_mask}() = \begin{cases} 0x0000, & \text{if } \text{Fqfreeze}() \geq 0 \\ 0xffff, & \text{if } \text{Fqfreeze}() < 0 \end{cases}$$

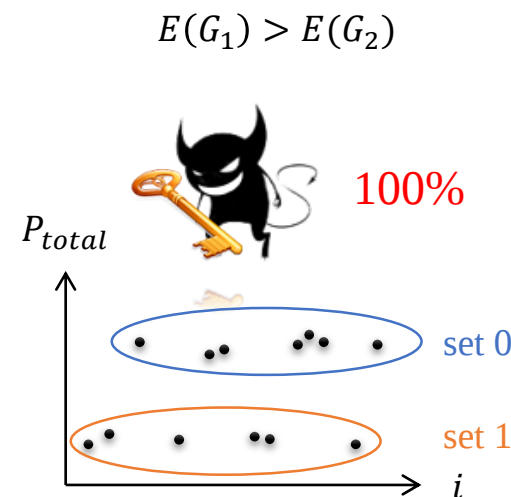
$$r[i] = \begin{cases} 0, & \text{if } \text{int16_negative_mask}() = 0x0000 \\ 1, & \text{if } \text{int16_negative_mask}() = 0xffff \end{cases}$$

■ NTRU Prime / LPRime : Distributions of the Pols



Optimization Level	$E(G_1)$	$E(G_2)$	$ E(G_1) - E(G_2) $
-O0	7.6411e-02	3.0403e-02	4.6008e-02
-O1	-4.2961e-02	-7.8910e-02	3.5949e-02
-O2	-6.6894e-02	4.0483e-02	2.6411e-02
-O3	4.9231e-02	2.8530e-02	2.0701e-02
-Os	-4.6974e-02	-8.8565e-02	4.1591e-02

k-means clustering algorithm



qTESLA

❖ Attack Scenario

Public key (pk), Secret key (sk)

Message m , Signature ($Sign$)

$$(y_i)_{0 \leq i \leq N} \leftarrow \text{Sample}()$$

$$(v_i)_{0 \leq i \leq N} \leftarrow a \cdot (y_i)_{0 \leq i \leq N}$$

$$\star c \leftarrow \text{Enc}(H([(v_i)_{0 \leq i \leq N}]_M, m))$$

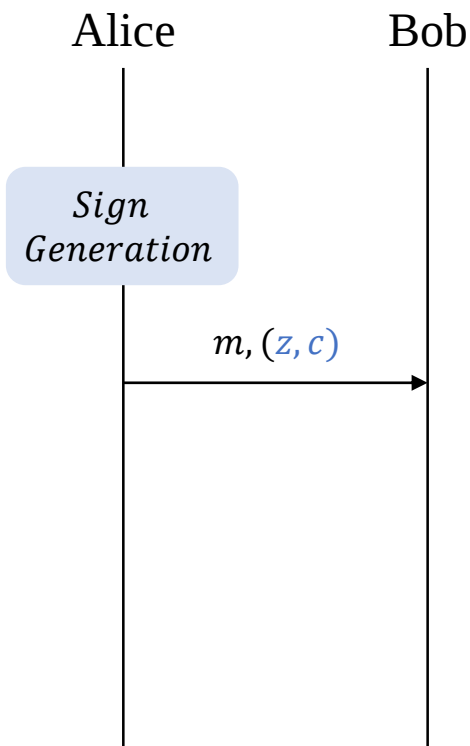
$$(z_i)_{0 \leq i \leq N} \leftarrow (y_i)_{0 \leq i \leq N} + (s_i)_{0 \leq i \leq N} \cdot c$$

$$(w_i)_{0 \leq i \leq N} \leftarrow (v_i)_{0 \leq i \leq N} - (e_i)_{0 \leq i \leq N} \cdot c$$

$$z \leftarrow (z_i)_{0 \leq i \leq N}$$



Single-Trace Attack



$$\star N + 1 \text{ Share. } x = x_0 \oplus \cdots \oplus x_N, (x_i)_{0 \leq i \leq N}$$

■ qTESLA : ML-based TA (Machine Learning based Template Attack)

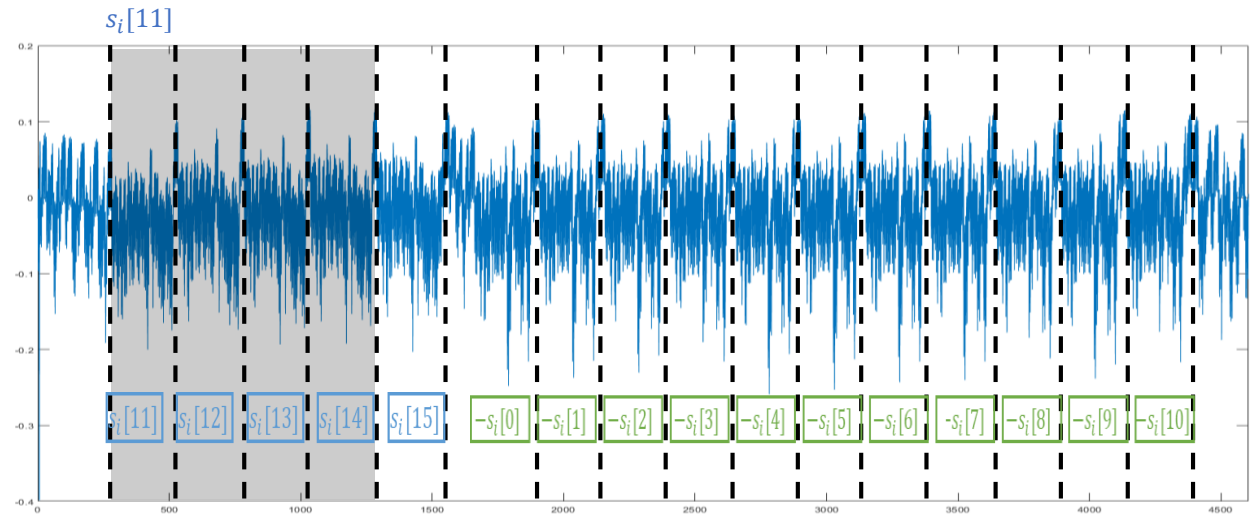
START

공격 파형, 서명 값 획득


 학습 파형 생성

학습 단계

공격 단계



degree	x^0	x^1	x^2	x^3	x^4	x^5	x^6	x^7	x^8	x^9	x^{10}	x^{11}	x^{12}	x^{13}	x^{14}	x^{15}
c						<i>Sparse</i> -1										
s_i	$s_i[0]$	$s_i[1]$	$s_i[2]$	$s_i[3]$	$s_i[4]$	$s_i[5]$	$s_i[6]$	$s_i[7]$	$s_i[8]$	$s_i[9]$	$s_i[10]$	$s_i[11]$	$s_i[12]$	$s_i[13]$	$s_i[14]$	$s_i[15]$

❖ 학습 파형 (곱셈 연산 4개)

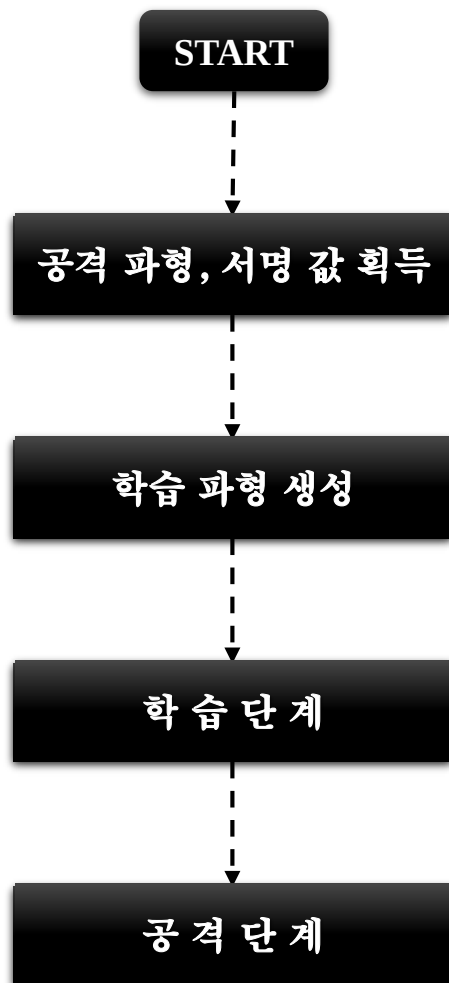
❖ Label : $s_i[j]$ value

❖ Model : MLP

 $s_i[j] : 16\text{bit}$

상위 8bit	하위 8bit
---------	---------

■ qTESLA : ML-based TA (Machine Learning based Template Attack)



Layer	Node (in, out)	Kernel initializer
Input Layer	(x, x)	-
Batch Normalization	(x, x)	-
Dense	$(x, 64)$	he_uniform
Relu	$(64, 64)$	-
Batch Normalization	$(64, 64)$	-
Dense	$(64, 64)$	he_uniform
Relu	$(64, 64)$	-
Batch Normalization	$(64, 64)$	-
Dense	$(64, 256)$	he_uniform
Softmax	$(256, 256)$	-

- Input Normalization: all values are within the range of -1 and 1
- Loss function: categorical_crossentropy
- Optimizer: Nadam (lr=0.002, epsilon=1e-08)
- Label encoding: one-hot encoding
- Batch size and epochs: 32 and maximum 100, respectively
- #Trace: (training T , validation V)



Masked qTESLA
Secret (s, e)

$$s = s_0 \oplus s_1 \oplus s_2 \oplus \dots \oplus s_N$$

$$t = a \cdot s + e \quad \longrightarrow \quad e = t - a \cdot s$$

Single-Trace Attack

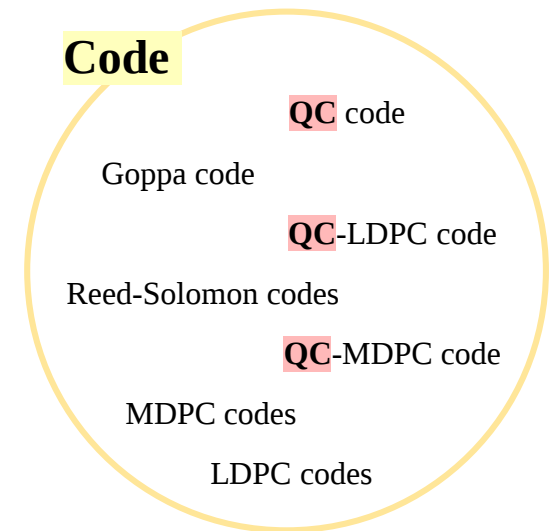
■ NIST Round 2 Code

❖ QC code based cryptosystem

Algorithm		Purpose	Code
BIKE		KEM	QC-MDPC
HQC		KEM-DEM	QC & BCH
RQC		KEM-DEM	QC & Gabidulin
LEDAcrypt	LEDAkem	KEM	QC-LDPC
	LEDApkc	KEM	QC-LDPC

❖ other code based cryptosystem

Algorithm		Purpose	Code
Classic McEliece		KEM	Goppa
NTS-KEM		KEM	Goppa
ROLLO(LAKE, LOCKER, Ouroboros-R)		KEM-DEM	LRPC



- **Quasi-Cyclic** code for saving memory (small key sizes)

SCA on KEM/PKE

+	[PQCrypto 2008]
—	[ICISC 2009]
—	[PQCrypto 2010]
—	[PQCrypto 2010]
FA	[FutureTech 2010]
—	[J. Cryptographic Engineering 2011]
—	[J. Cryptographic Engineering 2011]
—	[J. Cryptographic Engineering 2011]
—	[PQCrypto 2013]
↓	[RadioElektronika 2015]

공격 대상	공격 연산	공격 유형	대응 기법
McEliece	Decryption (Patterson algorithm / Error locator polynomial)	TA	Raise degree
	Key Generation (Generation of parity-check matrix)	PA	Masking
	Decryption (Permutation)	MA	Constant-time operation, only public input dependent access
McEliece	Decryption (Patterson algorithm / Error locator polynomial)	TA	Regular operation
McEliece	Decryption (Patterson algorithm / Secret permutation)	TA	Regular operation
McEliece	Decryption (Permutation, syndrome computation, syndrome inversion)		Shuffling, insert dummy, masking
McEliece	Decryption (Patterson algorithm / Error locator polynomial)	SPA	Regular operation
McEliece	Decryption (Root finding)	TA / FA	Regular operation, blinding, masking
McEliece / Niederreiter	Decryption (Patterson algorithm / Error locator polynomial)	TA	
McEliece	Decryption (Syndrome inversion)	TA ^C	
McEliece	Decryption (Syndrome computation)	SPA	Regular operation

Patterson algorithm

SCA on KEM/PKE

공격 대상	공격 연산	공격 유형	대응 기법
McEliece	Decryption (Permutation)	DPA	Masking
McEliece	Decryption (Patterson algorithm / Error locator polynomial)	TA	Regular operation
QC-MDPC McEliece	Encryption (Matrix multiplication) / Decryption (Key rotation)	TA, SPA	Regular operation
QC-MDPC McEliece	Decryption (Syndrome computation / key rotation)	DPA + Algebraic	Masking
QC-MDPC McEliece	Decryption (Syndrome computation / key rotation)	DPA + Algebraic	Masking
QC-MDPC McEliece	Decryption (Syndrome computation, decoder)		Masking
QC-MDPC	Decryption (Syndrome computation)		Regular operation
QC-MDPC	Decryption (Syndrome computation)	DPA + Algebraic	Masking
QC-MDPC	Decryption (Syndrome computation)		Masking
QC	Decryption (Syndrome computation)	DPA, SPA	Masking, hiding(mentioned)

[RadioElektronika 2016]

[J. Computers, Communications & Control 2017]

[ICCCC 2018]

[PQCrypto 2014]

[ACNS 2015]

[IEEE Transactions 2016]

[SAC 2016]

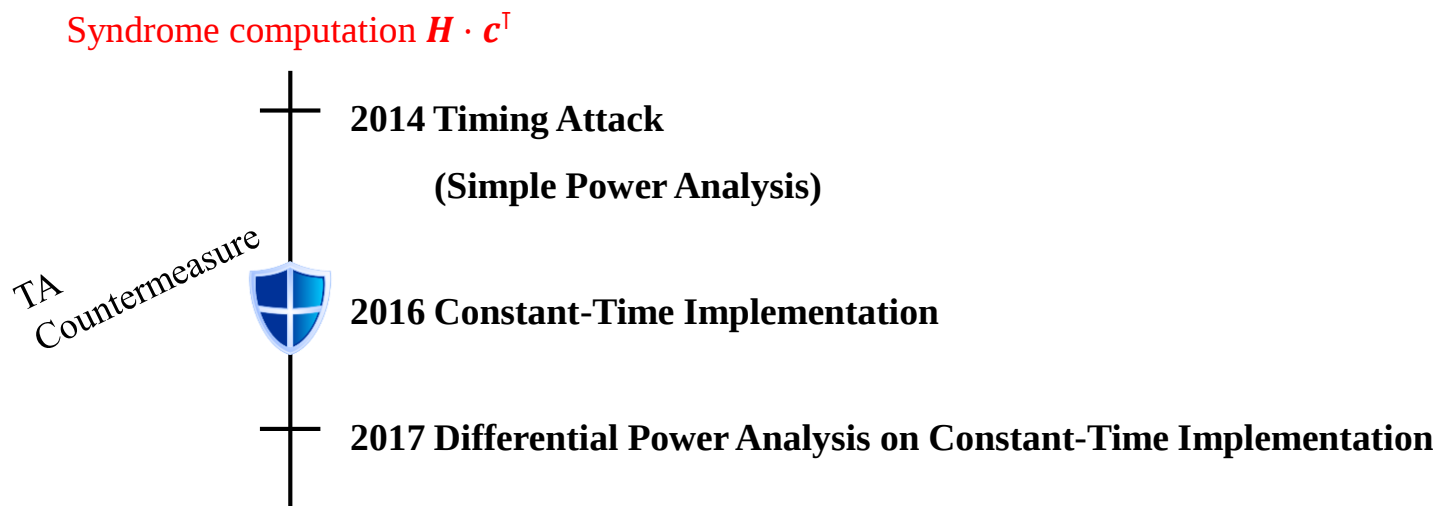
[CHES 2016]

[CHES 2017]

[TIIS 2019]

[TCHES 2019]

■ [CHES 2017] A side-channel assisted cryptanalytic attack against QcBits



Limitation: It could not completely recover accurate secret indices, requiring further **solving linear equations** to obtain entire secret information

↓

	8-bit	16-bit	32-bit	64-bit
80-bit security	0.4 seconds	15 seconds	16 hours	≈ 530 years
128-bit security	2 seconds	4 minutes	≈ 7 days	≈ 790,000 years

It is not feasible on 64-bit processor

■ Multiple-Trace Attack on Constant-Time Multiplication

$$d = (d_7 d_6 d_5 d_4 d_3 d_2 d_1 d_0)_2$$

8-bit word

Correlation
Occurring
Position

Correlation
Power
Analysis

Word unit rotation

$$result = \begin{cases} unrotated & , if d_i = 0 \\ rotated & , if d_i = 1 \end{cases}$$

$$result = \begin{cases} (rotated \& \mathbf{0x00}) \oplus (unrotated \& \mathbf{0xff}) = unrotated & , if d_i = 0 \\ (rotated \& \mathbf{0xff}) \oplus (unrotated \& \mathbf{0x00}) = rotated & , if d_i = 1 \end{cases}$$

Bit rotation

$$result = (\ll_{8-L}) | (\gg_L)$$

$$0 \leq L = (d_2 d_1 d_0)_2 < 8$$

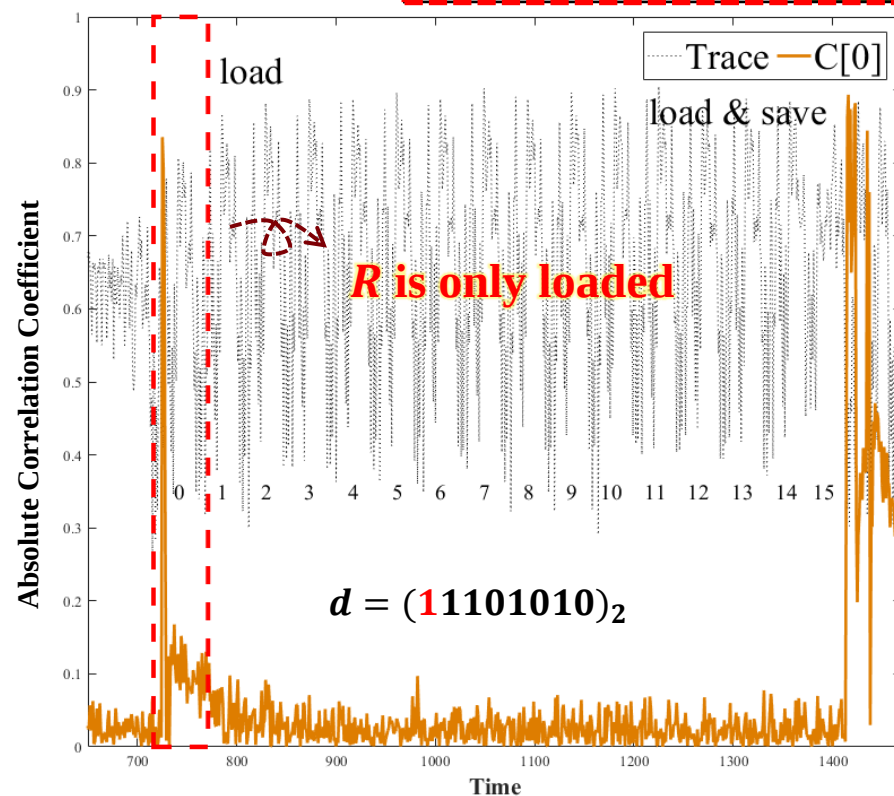
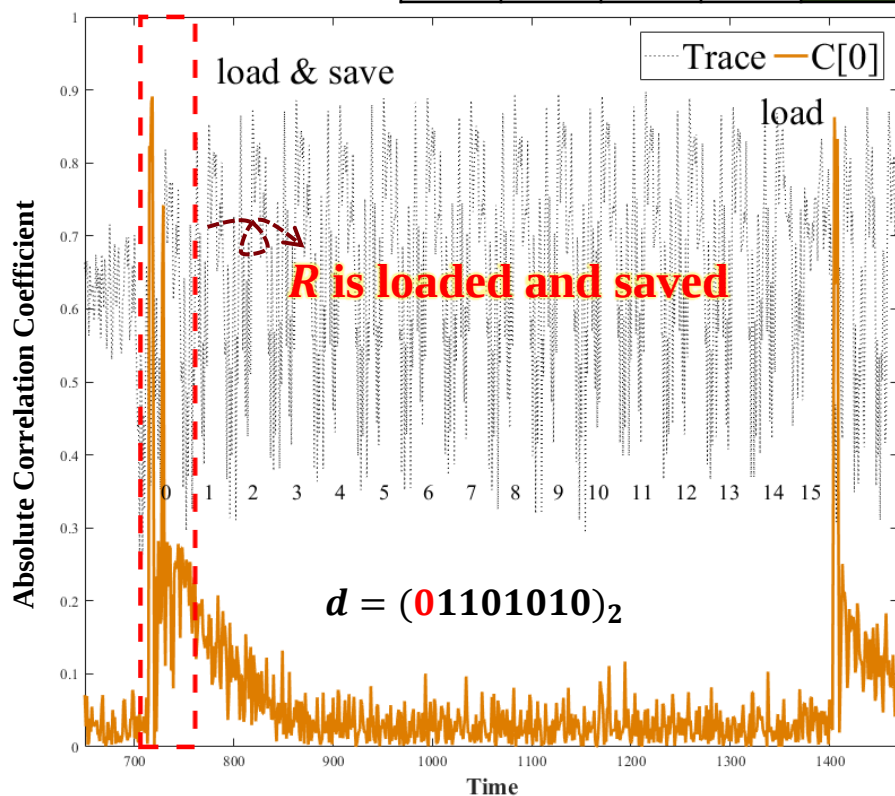
Property 1.

$$result = \begin{cases} unrotated & , if d_i = 0 \\ rotated & , if d_i = 1 \end{cases}$$

$$d = (\overbrace{d_7 d_6 d_5 d_4 d_3}^{\text{target}} d_2 d_1 d_0)_2, d_i \in \{0, 1\}$$

$$R \in_{Random} \{0, 1\}^8$$

8-bit word



Multiple-Trace Attack on the Word Unit Rotation

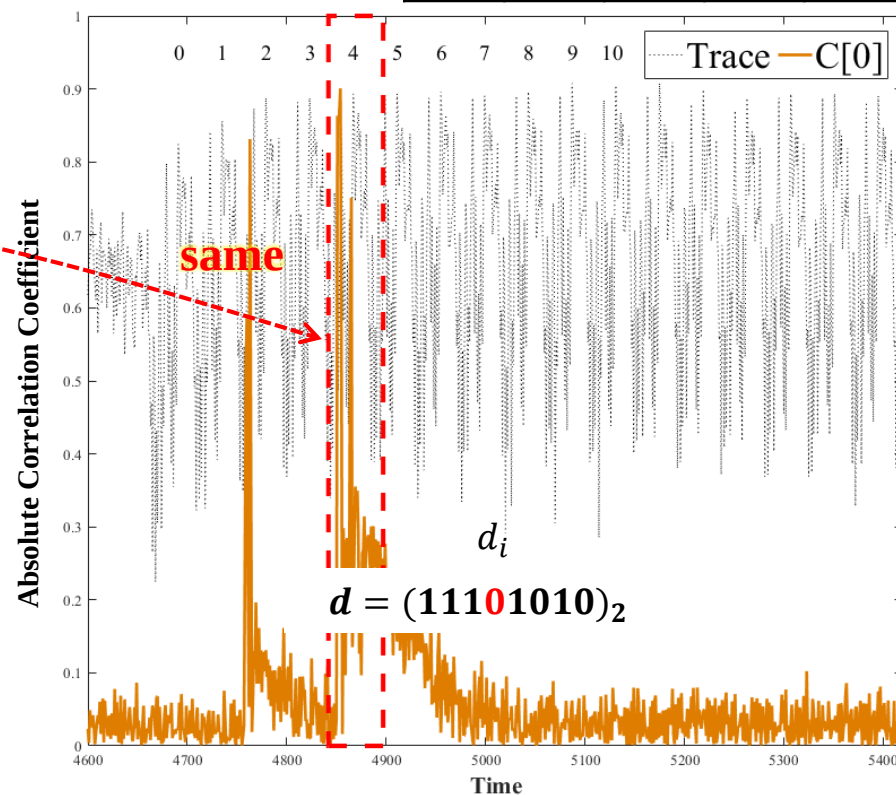
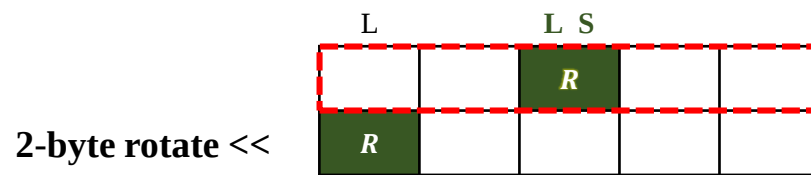
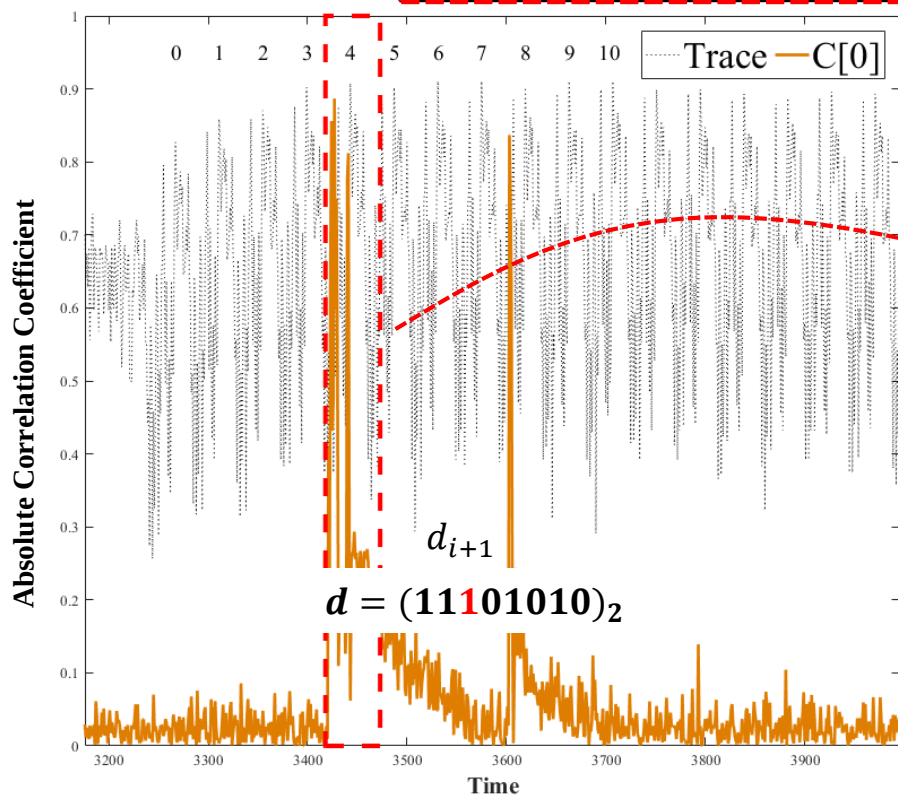
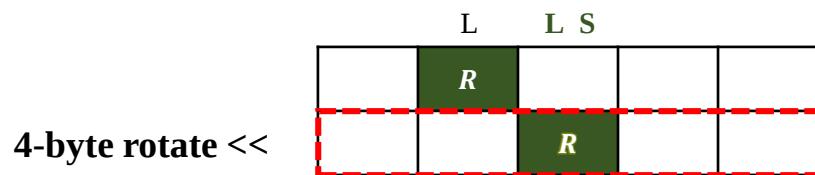
Property 2.

$$\text{result} = \begin{cases} \text{unrotated} & , \text{if } d_i = 0 \\ \text{rotated} & , \text{if } d_i = 1 \end{cases}$$

$$d = (\overset{\text{target}}{d_7 d_6 d_5 d_4 d_3 d_2 d_1 d_0})_2, d_i \in \{0, 1\}$$

$$R \in_{\text{Random}} \{0, 1\}^8$$

8-bit word



Multiple-Trace Attack on the Bit Rotation

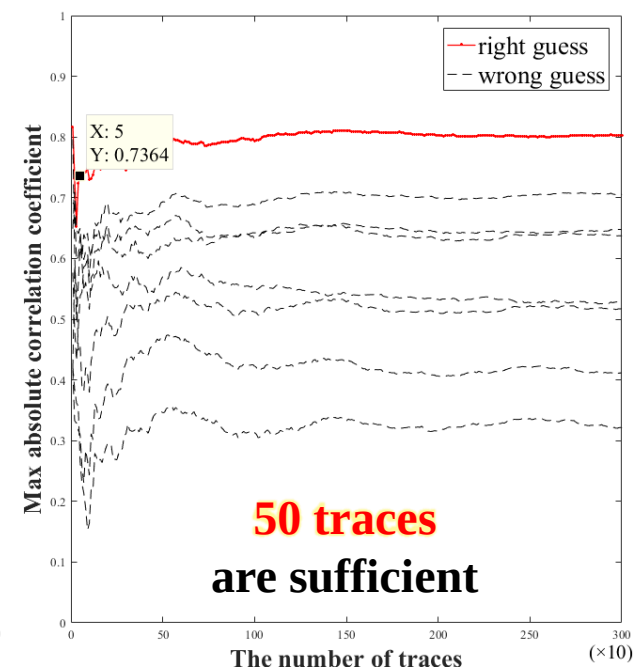
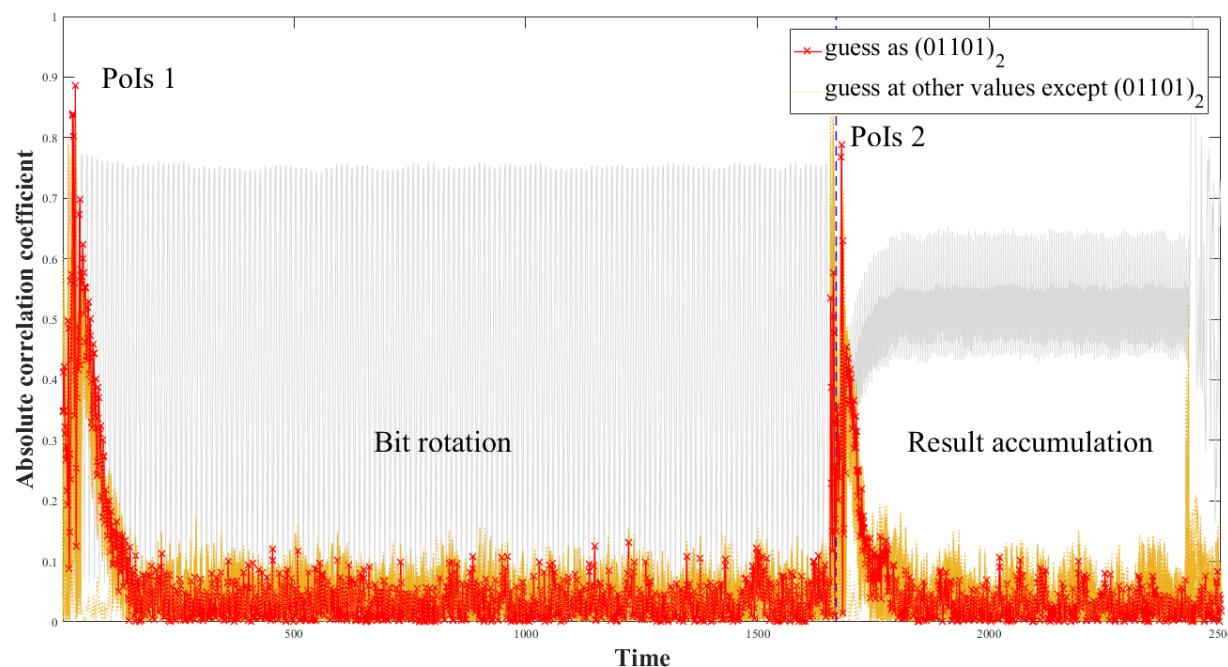
$$result = (\ll_{(8-L)} | (\gg_L))$$

$$0 \leq L = (d_2 d_1 d_0)_2 < 8$$

$$d = (\overset{\text{target}}{d_7 d_6 d_5 d_4 d_3 d_2 d_1 d_0})_2, d_i \in \{0, 1\}$$

8-bit word

- Guess the L value from 0 to 7
and calculate Pearson's correlation coefficient between traces and $result$ values



Single-Trace Attack on Constant-Time Multiplication

$$d = (d_7 d_6 d_5 d_4 d_3 d_2 d_1 d_0)_2$$

8-bit word

Key	Simple
Bit-dependent	Power
Attack	Analysis

Word unit rotation

$$result = \begin{cases} unrotated & , if d_i = 0 \\ rotated & , if d_i = 1 \end{cases}$$

$$result = \begin{cases} (rotated \& \textcolor{red}{0x00}) \oplus (unrotated \& \textcolor{red}{0xff}) = unrotated & , if \textcolor{red}{d_i} = 0 \\ (rotated \& \textcolor{blue}{0xff}) \oplus (unrotated \& \textcolor{blue}{0x00}) = rotated & , if \textcolor{blue}{d_i} = 1 \end{cases}$$

Bit rotation

$$result = (\ll_{8-L}) | (\gg_L)$$

$$0 \leq \textcolor{red}{L} = (d_2 d_1 d_0)_2 < 8$$

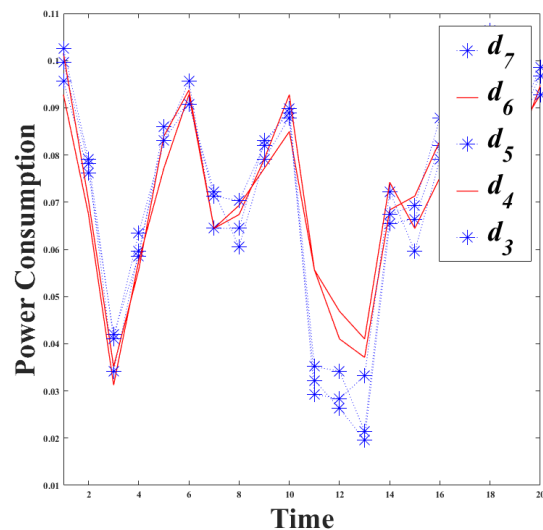
Single-Trace Attack on the Word Unit Rotation

$$d = (d_7 d_6 d_5 d_4 d_3 d_2 d_1 d_0)_2, d_i \in \{0, 1\}$$

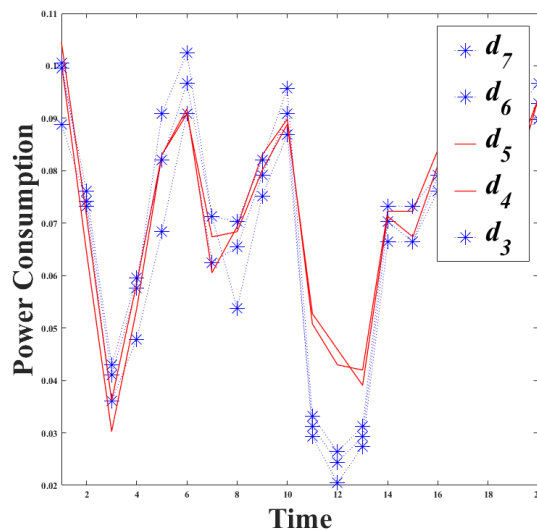
$$d = (\overbrace{d_7 d_6 d_5 d_4 d_3}^{\text{target}} d_2 d_1 d_0)_2, d_i \in \{0, 1\}$$

8-bit word

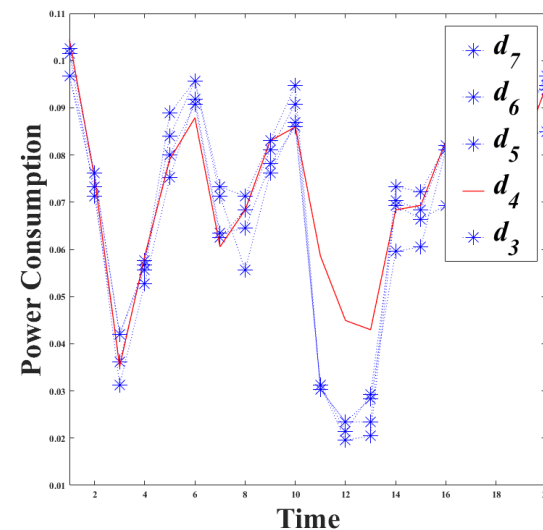
$$\text{result} = \begin{cases} (\text{rotated} \& \text{0x00}) \oplus (\text{unrotated} \& \text{0xff}) = \text{unrotated} & , \text{if } d_i = 0 \\ (\text{rotated} \& \text{0xff}) \oplus (\text{unrotated} \& \text{0x00}) = \text{rotated} & , \text{if } d_i = 1 \end{cases}$$



$$169 = (10101001)_2$$



$$201 = (11001001)_2$$



$$233 = (11101001)_2$$

Key Bit-dependent Property

$$\checkmark \quad W = 8$$

$$\text{mask} = \begin{cases} \text{0x00} & , \text{if } d_i = 0 \\ \text{0xff} & , \text{if } d_i = 1 \end{cases}$$

- K-means clustering
- Fuzzy k-means clustering
- EM (Expectation-maximization)

Single-Trace Attack on the Bit Rotation

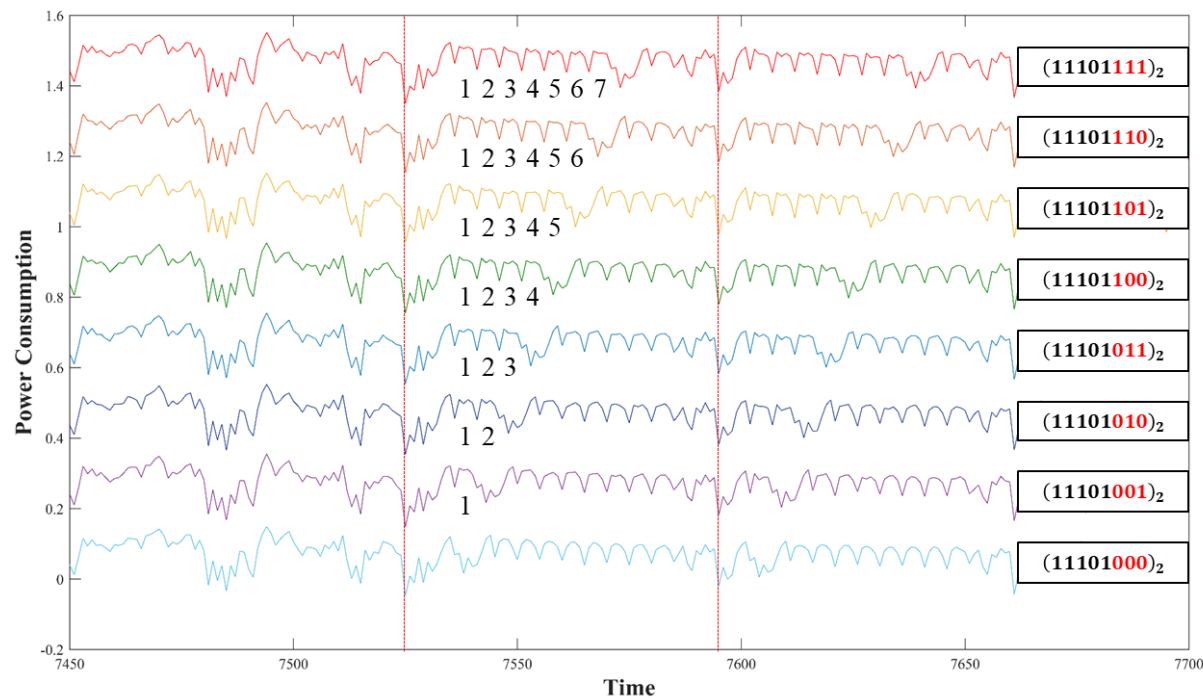
target

$$d = (d_7 d_6 d_5 d_4 d_3 \overbrace{d_2 d_1 d_0}^{\text{target}})_2, d_i \in \{0, 1\}$$

8-bit word

$$\text{result} = (\ll_{8-L}) | (\gg_L)$$

$$0 \leq L = (d_2 d_1 d_0)_2 < 8$$



Single-Trace Attack on the Bit Rotation

$$d = (d_7 d_6 d_5 d_4 d_3 \overbrace{d_2 d_1 d_0}^{\text{target}})_2, d_i \in \{0, 1\}$$

8-bit word

$$\text{result} = (\ll_{8-L}) | (\gg_L)$$

$$0 \leq L = (d_2 d_1 d_0)_2 < 8$$

	Bit rotate	Left shift	Right shift	SPA
AVR 8-bit word	Single bit shift instructions	$(8 - L)$ times (($8 - L$) clock cycles)	L times (L clock cycles)	O
MSP 16-bit word	Single bit shift instructions	$(8 - L)$ times (($8 - L$) clock cycles)	L times (L clock cycles)	O
ARM 32-bit word	Multiple bit shift instructions (ex. barrel shifter)	One clock	One clock	X
64-bit word	Multiple bit shift instructions (ex. barrel shifter)	One clock	One clock	X

✓ In the cases of 32-bit and 64-bit, we need to solve linear equations to find accurate indices

❑ Vulnerable operations

Loops whose bound is input-dependent

```
int j = 4;
for(i = 0; i < j; i++)
    ...

for(i = 0; i < length; i++)
    ... break;

for(i = 0; i < length; i++)
    ... exit;
```

```
int max_length = 6;
int j = 4;
for(i = 0; i < max_length; i++)
    determiner = ((i - j) & mask) >> 31;
```

Branches whose condition is input-dependent

```
if(i == 1)
    ... a=b;

if(j != 0)
    ... v=x;
else
    ... v=v;
```

```
determiner = !(((i-1) & mask) >> 31);
a = b * determiner;
determiner = -(((i-j) & mask) >> 31);
v = x * determiner + v * !determiner;
```

input-dependent memory access

```
for(i = 0; i < length; i++)
    if(i == index)
        ...
    a[i]=b[2i+1];
```

```
for(i = 0; i < length; i++)
    xorVal = i ^ index;
    determiner = (xorVal & 1) - 1;
    out = b[i] & determiner;
```

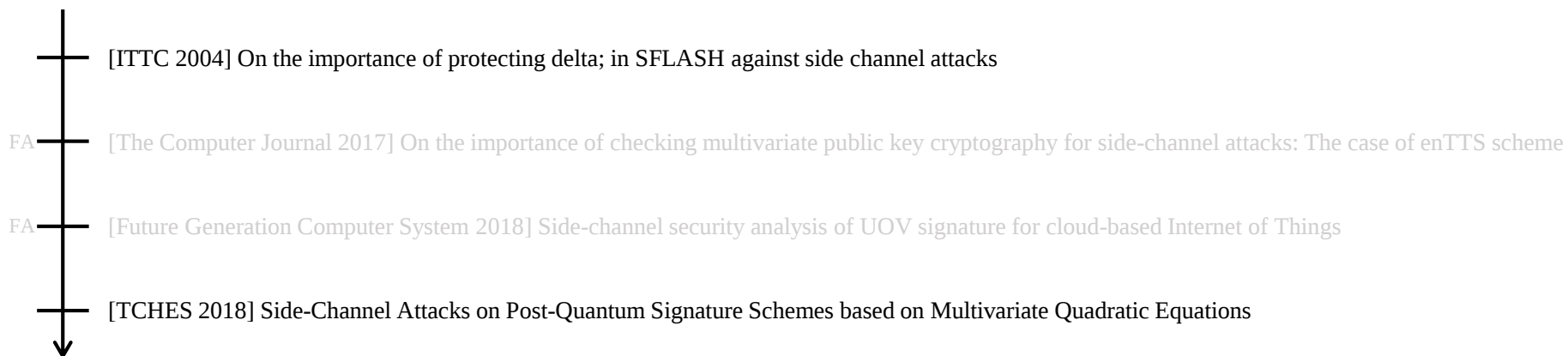
- ✓ Constant-time BCH Error-Correcting Code, ePrint 2019-155
- ✓ Timing Attack on HQC and Countermeasure, ePrint 2019-909

mask = 0xff; // 8-bit processor

■ NIST Round 2 Multivariate

Algorithm	Purpose	
GeMMS	Signature	HFE
LUOV	Signature	UOV
Rainbow	Signature	UOV
MQDSS	Signature	Fiat-Shamir

■ SCA on Signature



CPA against Rainbow Signature

❖ **Non-invasive** attack on MQ-based signature schemes

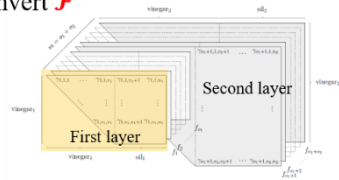
분석 대상

Rainbow Signature generation

Invert $\mathcal{S}$

$$\begin{pmatrix} s'_{11} & s'_{12} & \dots & s'_{1m} \\ s'_{21} & \ddots & \ddots & s'_{2m} \\ \vdots & \ddots & \ddots & \vdots \\ s'_{m1} & s'_{m2} & \dots & s'_{mm} \end{pmatrix} \begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_m \end{pmatrix}$$

Invert $\mathcal{F}$



Invert $\mathcal{T}$

$$\begin{pmatrix} t'_{11} & t'_{12} & \dots & t'_{1n} \\ t'_{21} & \ddots & \ddots & t'_{2n} \\ \vdots & \ddots & \ddots & \vdots \\ t'_{n1} & t'_{n2} & \dots & t'_{nn} \end{pmatrix} \begin{pmatrix} y'_1 \\ y'_2 \\ \vdots \\ y'_n \end{pmatrix}$$

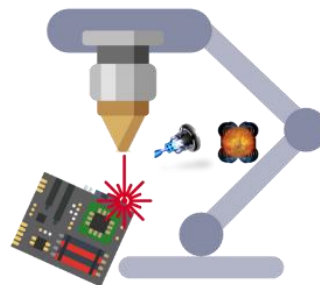
기존 연구

[The Computer Journal 2017]

CPA + **Fault** injection

✓ (Goal) **Recovery** the secret maps $\mathcal{S}, \mathcal{F}, \mathcal{T}$

enTTS implementation
with **random linear maps**



Fault Injection

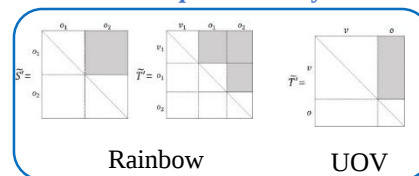
공격 가정 완화

제안 방법

CPA

✓ (Goal) **Recovery** the secret maps $\mathcal{S}, \mathcal{F}, \mathcal{T}$

Rainbow and UOV implementation
with **equivalent keys**



CPA + Algebraic

✓ (Goal) **forged** signature

Rainbow implementation
with **random linear maps**

Conclusion

KEM/Encryption

(9) Lattice-based		(7) Code-based	
FrodoKEM	LWE	Classic McEliece	Goppa
LAC	RLWE	NTS-KEM	Goppa
NewHope	RLWE	BIKE	Short Hamming
Round5	LWR/RLWR	HQC	Short Hamming
Crystals-Kyber	MLWE	LEDACrypt	Short Hamming
Saber	MLWR	RQC	Low rank
Three Bears	IMLWE	ROLLO	Low rank
NTRU	NTRU	(1) Isogeny	
NTRU Prime	NTRU	SIKE	Isogeny

Signature

(3) Lattice-based	
qTESLA	Fiat-Shamir
Crystals-Dilithium	Fiat-Shamir
FALCON	Hash then sign
(4) Multivariate	
GeMMS	HFE
LUOV	UOV
Rainbow	UOV
MQDSS	Fiat-Shamir
(2) Symmetric-based	
SPHINCS+	Hash
Picnic	ZKP

부채널 분석에 대한 안전성 검증 필요



Q & A

PA	Power Analysis
EMA	Electromagnetic Analysis
MA	Microarchitectural Attack
SPA	Simple Power Analysis
SPA ^P	Simple Power Analysis with Profiling
SEMA	Simple Electromagnetic Analysis
TA	Timing Attack
TA ^C	Cache Timing Attack ($\in$ MA)
TA ^P	Template Attack ($\in$ SPA ^P)
CA	Collision Attack
DPA	Differential Power Analysis
CPA	Correlation Power Analysis
CEMA	Correlation Electromagnetic Analysis
FA	Fault Attack
DFA	Differential Fault Attack
CBA	Cold Boot Attack

■ SCA on KEM/PKE

- [CT-RSA 2007] Timing attacks on NTRUEncrypt via variation in the number of hash calls
- [RFID Security 2008] Power analysis on NTRU implementations for RFIDs: First results
- [IEICE 2010] Countermeasures against Power Analysis Attacks for NTRU Public Key Cryptosystem
- [IEICE 2011] Fault analysis of the NTRUEncrypt cryptosystem
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