

Statistical Quantum Federated Learning for NOMA Power Allocation

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Abstract—This study employs the statistical Quantum Federated Learning (sQFL) to optimize NOMA power allocation. Compared to the existing Federated Learning (FL), sQFL does not require other edges to perform neural network inferences. The other edge only required to transmit the statistical information to the cloud.

Index Terms—Quantum neural networks, quantum federated learning, 6G, wireless communications.

I. INTRODUCTION

To maintain users' data privacy and distribute the computational load, federated learning (FL) can be employed to optimize the future wireless network [1]. Moreover, quantum computation has been studied to enhance the processing of machine learning [2]. The existing federated learning approach continuously includes the neural network of the "informant" in the training process [3].¹ To reduce the computation and communication burden of the "informant", this paper proposes a statistical quantum federated learning approach (sQFL). The sQFL only requires the "informant" to send the dataset statistics (without performing neural network inference).

Notations: Let \mathbf{H} , \mathbf{C}_Z , \mathbf{C}_X , \mathbf{R}_Z , and \mathbf{M} be the operation of Hadamard gate, controlled Z gate, controlled X gate, rotation on the Z axis, and quantum measurement, respectively. Let $x \sim \mathcal{CN}(\mu, \sigma^2)$, where μ and σ^2 denotes the mean and the variance, respectively be a complex Gaussian distribution. The notation of \otimes expresses Kocker product. The notations of \mathbb{R} and \mathbb{C} denote the real and complex numbers, respectively.

II. SYSTEM MODEL

Consider the m th radio access network (RAN) with a radio access point (RAP) for downlink (DL) non-orthogonal multiple access (NOMA). Consider $u_{\text{str}}^{[m]}$ and $u_{\text{weak}}^{[m]}$ as the user with a stronger and a weaker channel gain, accordingly. Let $d_{\text{str}}^{[m]}$ and $d_{\text{weak}}^{[m]}$ be the normalized distance values between the AP and $u_{\text{str}}^{[m]}$ and $u_{\text{weak}}^{[m]}$, respectively. Considering ρ as the transmit signal-to-noise ratio (SNR), the channel coefficients of $u_{\text{str}}^{[m]}$ and $u_{\text{weak}}^{[m]}$ are modeled as $h_{\text{str}}^{[m]} \sim \mathcal{CN}(0, (d_{\text{str}}^{[m]})^{-\vartheta})$ and $h_{\text{weak}}^{[m]} \sim \mathcal{CN}(0, (d_{\text{weak}}^{[m]})^{-\vartheta})$, respectively, where ϑ is the pathloss exponent [4]. The receive signal-to-interference-plus-noise-ratio (SINR) for $u_{\text{str}}^{[m]}$ and $u_{\text{weak}}^{[m]}$ can be expressed as $\gamma_{m,\text{str}}^{\text{NOMA}} = |h_{\text{str}}^{[m]}|^2 \rho \lambda_{\text{str}}^{[m]}$ and $\gamma_{m,\text{weak}}^{\text{NOMA}} = \frac{|h_{\text{weak}}^{[m]}|^2 \rho \lambda_{\text{weak}}^{[m]}}{|h_{\text{weak}}^{[m]}|^2 \rho \lambda_{\text{str}}^{[m]} + 1}$, respectively [5]. Subsequently, the sum rate of the NOMA users can be

¹For simplicity, this paper refers to the computing unit that processes the local dataset as the "informant." Let us refers to the computing unit that obtains the information from "informants" as "recipients."

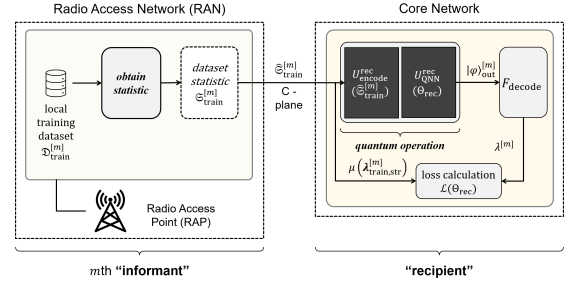


Figure 1: The proposed sQFL scheme.

expressed as $R_{m,\text{sum}}^{\text{NOMA}} = R_{m,\text{str}}^{\text{NOMA}} + R_{m,\text{weak}}^{\text{NOMA}}$, where the achievable rate of $u_{\text{str}}^{[m]}$ and $u_{\text{weak}}^{[m]}$ is defined as $R_{m,\text{str}}^{\text{NOMA}} = \log_2(1 + \gamma_{m,\text{str}}^{\text{NOMA}})$ and $R_{m,\text{weak}}^{\text{NOMA}} = \log_2(1 + \gamma_{m,\text{weak}}^{\text{NOMA}})$, accordingly. Finally, the objective of the NOMA power allocation optimization can be expressed as [6]:

$$\text{maximize}_{\lambda_{\text{str}}^{[m]}} \quad R_{m,\text{sum}}^{\text{NOMA}}(\lambda_{\text{str}}^{[m]}, \lambda_{\text{weak}}^{[m]} = 1 - \lambda_{\text{str}}^{[m]}) \quad (1a)$$

$$\text{subject to} \quad R_{m,\text{str}}^{\text{NOMA}} \geq R_{m,\text{str}}^{\text{OMA}}, R_{m,\text{weak}}^{\text{NOMA}} \geq R_{m,\text{weak}}^{\text{OMA}}, \quad (1b)$$

$$0 \leq \lambda_{n,\text{str}}^{\text{NOMA}} \leq 1, \quad (1c)$$

where the achievable rate of $u_{\text{str}}^{[m]}$ and $u_{\text{weak}}^{[m]}$ by utilizing orthogonal multiple access (OMA) is denoted as $R_{m,\text{str}}^{\text{OMA}}$ and $R_{m,\text{weak}}^{\text{OMA}}$, respectively.

III. PROPOSED SCHEME

The proposed sQFL (Fig. 1) can be described as follows. For this initial study, the presented scheme only considers one edge (therefore, no aggregation required).²

1) **Dataset Statistics:** Consider N_{info} as the number of the informants. Let $N_{\text{train}}^{[m]}$ be the number of training data for the m th informant, $m \in \{1, \dots, N_{\text{info}}\}$. Considering $k \triangleq \{h_{\text{train,str}}^{[m,j]}, h_{\text{train,weak}}^{[m,j]}, \lambda_{\text{train,str}}^{[m,j]}\}$ and $K \triangleq \{h_{\text{train,str}}^{[n]}, h_{\text{train,weak}}^{[n]}, \lambda_{\text{train,str}}^{[n]}\}$, the mean and standard deviation of the strong user channel, weak user channel, and strong user power allocation of the m th informant can be expressed as: $\mu(K) = \frac{1}{N_{\text{train}}^{[m]}} \sum_{j=1}^{N_{\text{train}}^{[m]}} k$ and $\sigma(K) = \sqrt{\frac{1}{N_{\text{train}}^{[m]}} \sum_{j=1}^{N_{\text{train}}^{[m]}} \lambda_{\text{train,str}}^{[m,j]} - \mu(K)^2}$, respectively. let the "range" of the confidence intervals to be expressed as

²This study considers that the quantum computation can be employed to complement the future network function. Moreover, this paper assumes that the QNN data can be communicated via the control plane (C-plane) [7].

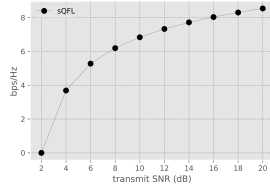


Figure 2: Initial simulation result.

$\Delta\varepsilon(\cdot) = |\varepsilon(\cdot)_2 - \varepsilon(\cdot)_1|$. The confidence intervals of power allocation are denoted as $\varepsilon_1(\lambda_{\text{train, str}}^{[m]}) = \mu(\lambda_{\text{train, str}}^{[m]}) - \varphi$ and $\varepsilon_2(\lambda_{\text{train, str}}^{[m]}) = \mu(\lambda_{\text{train, str}}^{[m]}) + \varphi$, where $\varphi \triangleq z_{\text{value}} \frac{\sigma(\lambda_{\text{train, str}}^{[m]})}{\sqrt{N_{\text{train}}^{[m]}}}$. z_{value} denotes the z-value.³ The dataset statistics of the m th edge can be concatenated by the recipient as a tuple of

$$\mathfrak{S}_{\text{train}}^{[m]} = [\Delta\varepsilon(\lambda_{\text{train, str}}^{[m]}); \{\mu(h_{\text{train, str}}^{[m]}), \sigma(h_{\text{train, str}}^{[m]})\}; \{\mu(h_{\text{train, weak}}^{[m]}), \sigma(h_{\text{train, weak}}^{[m]})\}; \{\mu(\lambda_{\text{train, str}}^{[m]}), \sigma(\lambda_{\text{train, str}}^{[m]})\}]. \quad (2)$$

2) *QNN Circuit*: The considered quantum neural network (QNN) circuit of the recipient can be described as follows. The encoding operation, which is based on [8], is expressed as $U_{\text{encode}}^{\text{rec}}(\mathfrak{S}_{\text{train}}^{[m]}) = \bigotimes_{n=1}^{N_{\text{info}}} \bigotimes_{i=1}^{|\mathfrak{S}_{\text{train}}^{[N_{\text{info}}]}|} \mathbf{R}_z(\tanh(x_i^{[m]})), x_i^{[m]} \in \mathfrak{S}_{\text{train}}^{[N_{\text{info}}]}$, where $x^{[m]}$ indicates the input values from n th informant (elements of $\mathfrak{S}_{\text{input}}^{[m]}$). Let Θ_{rec} and $|\mathfrak{S}_{\text{train}}^{[N_{\text{info}}]}|$ be the set of weights and number of elements of $\mathfrak{S}_{\text{train}}^{[m]}$, respectively. Consider $\tanh(\cdot)$ function as the pre-processing operation. Considering N_{layer} and N_{neuron} as the number of layers and neuron, respectively, the quantum dense layers (based on [9]) can be presented as

$$U_{\text{QNN}}^{\text{rec}}(\Theta_{\text{rec}}) = \left(\prod_{j=1}^{N_{\text{neuron}}^{[N_{\text{layer}}]} - 1} \mathbf{C}_Z(q_{N_{\text{layer}}, j+1}; q_{N_{\text{layer}}, j}) \right) U_A \left(\bigotimes_{l=1}^{N_{\text{layer}}} \bigotimes_{j=1}^{N_{\text{neuron}}^{[l]}} \mathbf{R}_z(\theta_{l,j}^{\text{rec}}) \right),$$

$$U_A \triangleq \begin{cases} \prod_{j=1}^{N_{\text{neuron}}^{[1]} - 1} \mathbf{C}_Z(q_{2,1}; q_{1,j}), & \text{for } l = 1, \\ \prod_{l=1}^{N_{\text{layer}} - 1} \mathbf{C}_X(q_{l+1,1}; q_{l, N_{\text{neuron}}^{[l]}}) \left(\prod_{j=1}^{N_{\text{neuron}}^{[l]} - 1} \mathbf{C}_Z(q_{l,j+1}; q_{l,j}) \right), & \text{for } 2 \leq l \leq N_{\text{layer}}, \end{cases} \quad (3)$$

where $\theta_{l,j}^{\text{rec}} \in \Theta_{\text{rec}}$ is the weight. Considering $|\psi\rangle_{\text{out}, r}^{[m]}$ as the output state of $U_{\text{QNN}}^{\text{rec}}(\Theta_{\text{rec}})$ for the r th quantum measurement, the decoding function can be expressed as $F_{\text{decode}}(|\psi\rangle_{\text{out}}^{[m]}) = \frac{1}{N_{\text{measure}}} \sum_{r=1}^{N_{\text{measure}}} \mathbf{M}(|\psi\rangle_{\text{out}, r}^{[m]})$, where N_{measure} is the number of quantum measurements and $|\psi\rangle_{\text{out}}^{[m]} = \{|\psi\rangle_{\text{out}, 1}^{[m]}, \dots, |\psi\rangle_{\text{out}, N_{\text{measure}}}^{[m]}\}$. Subsequently, consider $\lambda_{\text{str}}^{[m]} = F_{\text{decode}}(|\psi\rangle_{\text{out}}^{[m]})$.

3) *Initial Result*: A simply iterative training (Algorithm 1) is employed for this initial study. Let \mathcal{W} as the set of weight options, where the i th weight options ($w \in \mathcal{W}$) can be expressed as $\omega_i = -2\pi + (i-1)\frac{2\pi}{N_{\omega}}$, where $\omega_i \leq 2\pi$ and $l \geq 1$. The quantum operations ($U_{\text{encode}}^{\text{rec}}$ and $U_{\text{QNN}}^{\text{rec}}$) were performed

Algorithm 1 Training

Output: Optimized Θ_{rec} .

Initialization:

1: Set all qubits in $U_{\text{encode}}^{\text{rec}}$ and $U_{\text{QNN}}^{\text{rec}}$ to $|0\rangle$. Set all weights in Θ_{rec} to 0.

Training:

2: Calculate $\mathfrak{S}_{\text{train}}^{[m]}$ (Eq. (2)).

3: **for** each weight in Θ_{rec} **do**

4: **for** all weight options **do**

5: Consecutively, perform $U_{\text{encode}}^{\text{rec}}$, $U_{\text{QNN}}^{\text{rec}}$, and F_{decode} to obtain $\lambda_{\text{str}}^{[m]}$ (Section III-2).

6: Calculate loss $\mathcal{L}(\Theta_{\text{rec}}) = |\lambda_{\text{str}}^{[m]} - \mu(\lambda_{\text{train, str}}^{[m]})|^2$.

7: **end for**

8: Determine $\theta_{l,j}^{\text{rec}} = \arg \min_{\theta_{l,j}^{\text{rec}} \in \Theta_{\text{rec}}} \mathcal{L}(\Theta_{\text{rec}})$.

9: **end for**

using IBM Q (using IBM Qiskit [10]), where $N_{\text{measure}} = 1024$ were considered. The simulation parameters are considered as follows: $\vartheta = 2$ and $N_{\text{data}} = 100$. For each j th training data, $j \in \{1, \dots, N_{\text{train}}^{[m]}\}$, the power allocation coefficient is obtained as $\lambda_{\text{train, str}}^{[m,j]} = \frac{\sqrt{1 + (\|h_{\text{train, str}}^{[m,j]}\|^2 \rho) - 1}}{\|h_{\text{train, str}}^{[m,j]}\|^2 \rho}$, [6].⁴ The average result of Monte-Carlo simulation (10^4 trials) is presented in Fig. 2.

Future Work: The future work can consider other data statistics.

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³For instance, $z_{\text{value}} = 1.96$ is employed for 95% confidence level.

⁴For simplicity, this paper assumes $\rho = 10$ dB for all training data.